Variations of Kelvin waves around the TTL region during the stratospheric sudden warming events in the Northern Hemisphere winter

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Abstract. Spatial and temporal variabilities of Kelvin waves during stratospheric sudden warming (SSW) events are investigated by the ERA-Interim reanalysis data, and the results are validated by the COSMIC temperature data. A case study on an exceptionally large SSW event in 2009, and a composite analysis comprising 18 events from 1980 to 2013 are presented. During SSW events, the average temperature increases by 20 K in the polar stratosphere, while the temperature in the tropical stratosphere decreases by about 4 K. Kelvin wave with wave numbers 1 and 2, and periods 10–20 days, clearly appear around the tropical tropopause layer (TTL) during SSWs. The Kelvin wave activity shows obvious coupling with the convection localized in the India Ocean and western Pacific (Indo-Pacific) region. Detailed analysis suggests that the enhanced meridional circulation driven by the extratropical planetary wave forcing during SSW events leads to tropical upwelling, which further produces temperature decrease in the tropical stratosphere. The tropical upwelling and cooling consequently result in enhancement of convection in the equatorial region, which excites the strong Kelvin wave activity. In addition, we investigated the Kelvin wave acceleration to the eastward zonal wind anomalies in the equatorial stratosphere during SSW events. The composite analysis shows that the proportion of Kelvin wave contribution ranges from 5 to 35\% during SSWs, much larger than in the non-SSW mid-winters (less than 5\% in the stratosphere). However, the Kelvin wave alone is insufficient to drive the equatorial eastward zonal wind anomalies during the SSW events, which suggests that the effects of other types of equatorial waves may not be neglected.

Keywords. Meteorology and atmospheric dynamics (middle atmosphere dynamics; waves and tides)

1 Introduction

Atmospheric Kelvin waves were first suggested by Matsuno (1966), and they are confined in the latitude range between 20° S and 20° N with no meridional components (Andrews et al., 1987). They are eastward propagating equatorial waves excited by tropical convection (Bergman and Salby, 1994), and are the most prominent components of the equatorially trapped wave mode of the temperature field (Tindall et al., 2006; Ern et al., 2008).

It was extensively accepted that the Kelvin waves are crucial in dynamic processes of equatorial atmosphere. They interact with the wind and play an important role in driving tropical quasi-biennial oscillation (QBO) by dissipation and transfer of momentum (Holton and Lindzen, 1972; Kawatani et al., 2009; Wallace and Kousky, 1968). Tropical tropopause layer (TTL) variability is also associated with Kelvin waves. Using simulations and global observational data, Ryu et al. (2008) found that the vertically propagating Kelvin waves play a pivotal role in the tropical tropopause height variability. Kelvin waves are also known in affecting the distribution of water vapor and the formation of clouds in the TTL region (Fujiwara et al., 2001; Zhou and Holton, 2002; Eguchi

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and Shiotani, 2004; Fueglistaler et al., 2009), even TTL upwelling is linked to the Kelvin waves (Ryu and Lee, 2010). Besides, Kelvin waves with shorter periods can propagate into the thermosphere and the ionosphere and then affect neutral and electron densities (Takahashi et al., 2007; Chang et al., 2010). More interestingly, Phanikumar et al. (2014) revealed ultra-fast Kelvin wave signatures in ionosphere during the polar stratospheric sudden warming (SSW) event in 2009, suggesting certain connections between Kelvin waves and SSWs.

Both spatial and temporal variations of the Kelvin waves have been investigated in detail by previous studies. Randel and Wu (2005) investigated the vertical variability of Kelvin waves and found that the maximum amplitudes of Kelvin waves were located near the tropopause. Alexander et al. (2008) and Suzuki et al. (2010) studied the longitudinal variability of Kelvin waves and suggested that some waves originated from the western hemisphere and propagated upward and eastward to South America. Alexander et al. (2008) also distinguished the monthly variability of Kelvin waves in 2007, and the strength of Kelvin wave was found to increase from February to March and suppress during September and October. Venkat Ratnam et al. (2006) discussed the annual variations of Kelvin wave activities, and reported that the maximum Kelvin wave strength was almost always observed in the Northern Hemisphere winter. Ern and Preusse (2009) calculated the Kelvin wave accelerations to the QBO and stated that peak accelerations accorded with the westerly shear phase. However, few attentions were paid to the variations of Kelvin waves during SSW events, even though hemispherical connections between these two phenomena have been notified.

The SSW is recognized as one of the most violent atmospheric phenomena, during which the temperatures in the polar stratosphere increase rapidly within a few days (Andrews et al., 1987). It affects the polar stratospheric thermal structure and circulation profoundly, and also has significant impacts on the regions from the troposphere to the thermosphere (Baldwin and Dunkerton, 2001; Liu and Roble, 2002; Thompson et al., 2002; Gong et al., 2013).

In addition to those influences on the polar atmosphere of the winter hemisphere, its associated effects could extend to the lower latitudes, affecting the dynamics from the tropical stratosphere (Manney et al., 2008) to the mesosphere and lower thermosphere (MLT) region (Sathishkumar et al., 2009; Lima et al., 2012), and even ionosphere (Jin et al., 2012; Gong et al., 2013). Fritz and Soules (1970) first revealed the lower temperature in the tropical stratosphere during an SSW event by satellite data. Several subsequent studies, both theoretical and observational, investigated the relationship between the tropical region and the SSW events (Garcia, 1987; Holton et al., 1995; Plumb and Eluszkiewicz, 1999; Randel et al., 2002; Vineeth et al., 2010; Yoshida and Yamazaki, 2011). These studies stated that the meridional circulation driven by the transient planetary wave forcing associated with polar SSWs can induce upwelling in the tropical region, in turn produce cooling in the stratosphere and upper troposphere in the tropical region during SSW events. Kodera (2006) found that the cooling in the equatorial lower stratosphere and upper troposphere during SSW could lead to an enhancement of convective activity near the tropical Southern Hemisphere (10°S–equator) and a suppression near the tropical Northern Hemisphere (5–10°N). Kuroda (2008) also suggested that the tropical convection tends to be enhanced during SSW. The variations of zonal wind have also been noticed (Pancheva et al., 2008; Yuan et al., 2012). Recently, Chandran and Collins (2014) studied the global effects of SSW on winds and found the eastward acceleration below 40 km and between 60 and 100 km, and westward acceleration within 40–60 km in the lower latitudes (equator–20°N). However, there are few studies on the response of the Kelvin waves to the SSWs, so no definite conclusions are drawn about the mechanisms through which the Kelvin waves and the SSWs are connected.

In the present paper, we extended the research by Kodera (2006) to study the features of Kelvin wave activity variability, especially around the TTL region, during the SSWs and attempted to present an explanation of the relationship between Kelvin wave and SSWs. To fulfill our goals, a case study was made on an exceptionally large SSW event in 2009 to investigate the typical features and a composite analysis was applied to reveal the common features of the Kelvin wave variability during the SSW events.

The data sets used in this study are described in Sect. 2. Section 3 shows the background changes during the SSW events. Section 4 presents the variations of Kelvin waves during SSW events. Discussions of several questions which arose in the previous sections are shown in Sect. 5, and conclusions are summarized in Sect. 6.

2 Data

In this study, we adopted the European Center for Medium Range Weather Forecasting (ECMWF) reanalysis (ERA-Interim) temperature and wind fields data. We also validated the results by the Constellation Observing System for Meteorology, Ionosphere, and Climate (COSMIC) satellites’ temperature data.

The ERA-Interim reanalysis is a gridded data set assimilating the observations and numerical weather prediction model output from 1979 to present (Dee et al., 2011). The ERA-Interim provides data of many atmosphere parameters (e.g. temperature, wind fields, humidity, etc.) for 37 standard pressure levels at 6 h intervals. In this study, we adopted the temperature, zonal wind, meridional wind, and vertical velocity data with a spatial resolution of 2.5°× 2.5° (latitude × longitude). Since our study focuses on the stratosphere and upper troposphere and to make it convenient to validate our results with the COSMIC Level 2
temperature data, we restricted the altitude range of the data within 200–5 hPa (11–37 km, roughly). A more detailed description and the whole data sets can be obtained from the ECMWF website (http://www.ecmwf.int/en/research/climate-reanalysis/era-interim).

The COSMIC Level 2 temperature profiles have a vertical resolution of 0.1 km. These data were provided by University Corporation of Atmospheric Research (UCAR) and processed by COSMIC Data Analysis and Archive Center (CDAAC). COSMIC constellation is constructed by six Low Earth Orbit (LEO) satellites with a 72° inclination and was launched in April 2006. COSMIC provides profiles of temperature, pressure, and humidity in the neutral atmosphere, and its excellent latitudinal coverage made it particularly useful for studying the global phenomena (Anthes et al., 2008). The altitude range of the temperature profiles is from near surface to 40 km, while we focus on the region above 10 km because of the inaccuracy in the lower altitude due to the humidity contributions. The accuracy of the temperature profiles above 10 km is sub-Kelvin (Schreiner et al., 2007; Wang and Alexander, 2009).

Besides, we also used the OLR data obtained from the National Oceanic and Atmospheric Administration (NOAA) (Liebmann and Smith, 1996) as a proxy for tropical convec-tions.

3 The tropical background during the SSW events

3.1 The SSW events identification

During the SSW events, the zonal mean temperature in the stratosphere of the polar region increases rapidly within a few days, meanwhile, the eastward zonal mean polar zonal wind decreases, and the SSW events can be identified as major ones if the eastward zonal mean polar zonal winds reverse to westward and minor ones do not reverse. With the long temporal coverage of ERA-Interim from 1979 to present, we identified the SSW events which occurred from 1979 to 2013 based on the features described above.

Previous studies (Matsuno, 1971; Manney et al., 2009) showed that the enhancement of extratropical planetary waves forcing is the cause of the SSW events. According to Andrews et al. (1987), the relationship between zonal mean zonal wind tendency (\( \frac{\partial \overline{u}}{\partial t} \)) and the extratropical planetary wave forcing can be approximately expressed as

\[
\frac{\partial \overline{u}}{\partial t} = f \overline{v^*} + \nabla \cdot F,
\]

where \( \overline{u} \) is the mean zonal wind, \( f \) is the Coriolis parameter, \( \overline{v^*} \) is the mean residual meridional wind, overbars denote the zonal mean. \( f \overline{v^*} \) represents the Coriolis force due to residual circulation, and \( \nabla \cdot F \) is the divergence of the Eliassen–Palm (\( E–P \)) flux which represents the planetary wave forcing. Similar to Kodera (2006), we choose the zonal mean zonal wind tendency to measure the strength of interaction between the planetary wave and the polar vortex during each selected SSW event. Using the ERA-Interim Reanalysis zonal wind data, the tendencies of zonal mean zonal wind at 10 hPa averaged between 60 and 90° N are calculated, and the day with the maximum deceleration is regarded as the central date (day 0) when the decreasing rate of zonal winds for each SSW event is the largest. The horizontal dashed lines in (a) correspond to 0 and \(-2 \text{ m s}^{-1} \text{ day}^{-1} \).

Figure 1a shows the time tendencies of these 19 identified events. It is clearly seen that the maximum deceleration values of zonal mean polar zonal wind of these events can exceed \(-2 \text{ m s}^{-1} \text{ day}^{-1} \) (positive eastward). The variations of zonal mean polar temperature and zonal wind at 10 hPa, which are averaged by all the identified events mentioned above from day \(-15 \) to day 15, are shown in Fig. 1b. The common features of the SSWs are well represented in the averaged event: the polar temperature during the composite event starts to increase from 203 K on day \(-8 \) and peaks (about 222 K) on day 3, while the polar eastward zonal wind
starts to decrease from 50 m s\(^{-1}\) on day \(-3\) and minimizes (about \(-5\) m s\(^{-1}\)) on day 3.

### 3.2 Tropical Changes during the SSW Events

#### 3.2.1 The 2009 SSW event

The 2009 event is documented as the strongest Arctic SSW event since 1979 (Harada et al., 2009), which would help to elucidate the typical features that our study focuses on. To study the variations in the tropical region during the SSW event, we analyzed the variations of extratropical planetary wave forcing, tropical temperature, tropical vertical velocity between 200 and 5 hPa using the ERA-Interim data, and the equatorial convection using OLR data. The temporal variations of those anomalous variables from day \(-15\) to day 15 during the 2009 event are presented in Fig. 2. The anomalies mentioned in the present study are calculated as the departure from the 31-day mean from day \(-15\) to day 15. The anomalies are further linearly detrended to remove the effects due to long timescale oscillations (e.g. QBO). We also applied a 5-day running mean to suppress day-to-day fluctuations. All these variables except vertical velocity are shown in both physical values (color shades) and values normalized by standard deviation (\(\sigma\)). The tropical vertical velocity is just shown in a normalized value because the physical value could vary more than two orders from the bottom to the top of the altitude range.

Figure 2a shows the eddy heat flux averaged between 40 and 70\(^\circ\)N, a region where the extratropical wave forcing is located. Since the zonal mean eddy heat flux of the planetary waves \(\overline{\vec{v}\vec{T}}\) (\(\vec{v}\) and \(\vec{T}\) are perturbations of meridional wind and temperature due to planetary waves) is proportional to the vertical component of \(E−P\) flux \(F_z = \frac{\rho_0 f_0}{\rho_f c_p} \overline{\vec{v}\vec{T}}\) (where \(\rho_0\) and \(\theta_0\) are the reference density and potential temperature, respectively), the \(\vec{v}\) is the perturbation of potential temperature due to planetary waves. \(z\) is the altitude, see Andrews et al. (1987), the \(\overline{\vec{v}\vec{T}}\) can be chosen as an indicator of extratropical wave forcing. We subtracted planetary scale wave components with zonal wave numbers \(k\) smaller than 4 (i.e. \(k = 1, 2, 3\)) (Hitchcock and Simpson, 2014) from extratropical meridional wind and temperature field, which were obtained from ERA-Interim Reanalysis between 200 and 5 hPa, to calculate the eddy heat flux. The overbar denotes zonal mean. Positive anomalies, which represent the enhancement of extratropical wave forcing, appear around day \(-10\) and become larger than 1\(\sigma\) around day \(-8\). Just as expected, the extratropical wave forcing peaks around day 0. Corresponding to the enhancement of wave forcing, the SSW event in the polar region is initiated.

Besides SSWs, the enhancement of extratropical wave forcing would simultaneously alter the hemispherical meridional circulation which, in turn, causes some changes in the tropical region (Garcia, 1987; Randel, 1993; Holton et al., 1995; Randel et al., 2002; Yoshida and Yamazaki, 2011). So we calculate the vertical velocity of the residual circulation in the tropical region (10\(^\circ\)S–10\(^\circ\)N), which would be helpful to illustrate the corresponding features associated with the wave forcing induced meridional circulation therein (Andrews et al., 1987; Garcia, 1987). According to Andrews et al. (1987), the vertical velocity of residual circulation \((\vec{w}^*)\) is defined as \(\vec{w}^* = \vec{w} + (a \cos \phi)^{-1} (\cos \phi \vec{\theta}^*/R_\phi) \phi\), where the overbars denote the zonal mean, subscripts denote partial differentiation, \(a\) is the Earth radius, \(\phi\) is latitude. The unit of the vertical velocity outcome is converted to Pa s\(^{-1}\) when we calculate the normalized value since the results are presented in pres-
sure coordinate. It is obviously shown that the upward vertical velocity anomalies larger than $1\sigma$ mainly appear around day $-5$ in the stratosphere above 100 hPa (Fig. 2b; note that the upward anomalous vertical velocity is negative in pressure coordinate), corresponding to the extratropical wave forcing enhancement. The enhanced upward anomalous vertical velocity represents the enhanced upwelling of the air masses in the tropical region, which could be induced by the meridional circulation. Following the increase of the tropical upwelling, a clear cooling of the tropical region ($10^\circ$S–$10^\circ$N) appears around day $-5$ (Fig. 2c). The temperature decreases about 4 K within 5 days and the negative anomalies are mainly located above 50 hPa. The cooling also occurs in the upper troposphere but the negative temperature anomalies vary less than $1\sigma$. The variation of the temperature is affected by both of the vertical velocity and the thermal forcing (Andrews et al., 1987; Kuroda and Kodera, 2004). However, since the wave forcing frequency is faster than that of the thermal forcing (Garcia, 1987; Randel et al., 2002), the response of tropical temperature, especially in the stratosphere, to the wave forcing could be regarded as adiabatic, which means the temperature tendency and vertical velocity in the tropical region during the SSW are roughly related as $\frac{\partial T}{\partial t}\approx -\Gamma \Omega^2$, $\Gamma$ is a factor of static ability. When the upwelling in the tropical region enhances, the air masses ascend and expand adiabatically, as a result, the tropical temperature in the stratosphere would decrease.

Figure 2d depicts the time series of the zonal mean anomalous OLR (the lower OLR data correspond to higher convective activity, note that the y axis is reversed so that the peak and/or valley of the time series corresponds to the peak and/or valley of the convection). The anomalous OLR starts to decrease rapidly from about day $-8$ and the negative value less than $1\sigma$ appear on day $-1$. The OLR reaches the minimum on day 1, after which the tropical convection decreases and returns to the pre-warming level around day 10 (absolute value less than $1\sigma$). The variation of OLR data suggests that the zonal mean convection in the equatorial region is enhanced during the SSW event. Previous studies suggested that the convection enhancement is connected to the enhanced upwelling through convergence of air mass and water vapor in the troposphere during SSW events (Collimore et al., 2003; Eguchi and Kodera, 2007). The enhancements of the tropical convection which occurred during the SSW events, implying more equatorial waves could be excited during SSWs, have also been reported by previous works (Kodera and Yamada, 2004; Kodera, 2006, 2008).

### 3.2.2 Composite event

The composite analysis is applied to study the common features of tropical variations during the SSW events. The composite event is averaged by all the identified events listed in Table 1 except for the 2009 event, which would undermine the robustness of the composite analysis if it is included. To reveal the robustness of the composite results, a Student $t$ test is applied. The Student $t$ value is defined as follows:

$$t = x/(\sigma/n^{1/2}),$$

where $n$ is the number of the samples included in the composite analysis, $x$ is the mean over the 18 samples, and $\sigma$ is the standard deviation as mentioned above. In this study, the values corresponding to a 95% significance level for one-sided and two-sided tests are 1.73 and 2.10, respectively. So the Student $t$ absolute values exceeding 2 are chosen to illustrate the significant part.

As shown in Fig. 3, the variations of an extratropical eddy heat flux, tropical vertical velocity of residual circulation, tropical temperature, and tropical OLR in the composite event shared almost the same features with those in the 2009 SSW event, indicating that the tropical variations are identical during the SSW events. Though the enhancements of tropical convection during the SSW events is valid, the connection between the enhanced residual circulation and the tropical convection might be questioned since the tropical changes of vertical velocity and temperature are significant mainly above 50 hPa, which is consistent to the previous studies (Ueyama et al., 2013; Abalos et al., 2014). In fact, recent studies by Kodera et al. (2015) have stated that the influence of the enhanced residual circulation could penetrate downward into the troposphere through the change of cloud formation during SSW events, further strengthening the equatorial convection. Besides, our composite results are consistent with the results of Kodera (2006).

Briefly summarizing the descriptions of this section, we know that the extratropical wave forcing causes the SSW in the polar region, and simultaneously drives the meridional

<table>
<thead>
<tr>
<th>Year of the SSW events</th>
<th>Central date</th>
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<tbody>
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<td>1981</td>
<td>29 January</td>
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<tr>
<td>1984</td>
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<td>1984</td>
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circulation. The enhanced meridional circulation, in turn, induces the tropical upwelling, which causes the temperature decrease in stratosphere and upper troposphere in the tropical region. The influence of the enhanced tropical upwelling would also penetrate downward into the troposphere and enhance the tropical convection, which would further excite more equatorial waves. Thus, we may conclude that the SSW event in the polar region and the tropical changes, especially the enhancement of equatorial waves, are two individual results due to the extratropical planetary wave forcing.

4 Kelvin waves during the SSW events

4.1 Extraction of Kelvin waves

In this study, we focus on the variations of Kelvin wave during the SSWs and the certain connections between them. To extract Kelvin wave components, we applied a space-time spectral analysis to the temperature perturbations \( T' \), which are calculated as departure from zonal mean daily temperature at each height for each day. As described by Ern et al. (2008), in the space-time spectral analysis, the temperature perturbations are first divided into symmetric and antisymmetric components with respect to the equator:

\[
T'(\phi) = 0.5 \times [T'(\phi) + T'(-\phi)] + 0.5 \times [T'(\phi) - T'(-\phi)] = T_s'(\phi) + T_a'(\phi),
\]

where \( \phi \) is latitude, \( T_s'(\phi) \) and \( T_a'(\phi) \) are symmetric and antisymmetric components of the temperature perturbations, respectively. At fixed latitude, the temperature perturbations are a function of longitude and time. Then, we apply a 2-D Fourier transform to obtain wavenumber-frequency spectra of the symmetric/antisymmetric temperature components. It should be noted that, in order to apply 2-D Fourier transform mentioned above, the data grids must be even. So, before calculating temperature perturbations \( T' \), the uneven COSMIC data (15° S–15° N) are first binned into non-overlapped 5° × 15° (latitude × longitude) grid cells with temporal resolution of 1 day. The temperature data averaged within one grid cell are regarded as the data at the grid center. Thus, we obtain COSMIC temperature data on five latitude bands centering on 10° S/N, 5° S/N and 0° and each band has 24 grids in longitude. The ERA-Interim Reanalysis data are binned into the same latitude bands with COSMIC data while the longitude width of each grid cell is kept original (i.e. 2.5°).

Since the Kelvin waves are large-scale components (mostly with zonal wavenumber \( s = 1, 2, 3 \)), the different longitude width of the two data sets will not have much of an effect on the result.

Temperature field of Kelvin waves is in the symmetric mode (Andrews et al., 1987; Tindall et al., 2006), and according to the dispersion relation (Ern and Preusse, 2009; Matsuno, 1966), Kelvin wave components with different wave numbers and frequencies are extracted from the symmetric spectra by band pass filtering. The filtering region of Kelvin wave in the spectra is recognized by the different equivalent depth (Wheeler and Kiladis, 1999), corresponding to different phase speed of Kelvin waves (\( c_s = \sqrt{g \rho_e} \), where \( g \) is the gravitational acceleration). Since the altitude range in our study is restricted to the upper troposphere and lower stratosphere, according to Alexander et al. (2008), the band of within this altitude range is restricted to 8 m < \( h_e < 240 \) m (about 9 m s\(^{-1}\) < \( c_s < 50 \) m s\(^{-1}\)).

The spectral analysis and extraction method described above are applied to the ERA-Interim reanalysis data and COSMIC data in a SSW duration, from day −15 to day 15
The normalized wavenumber and/or frequency spectra of the symmetric temperature perturbations using ERA-Interim reanalysis data (a, d, g), the time–longitude cross section of Kelvin wave variances derived from ERA-Interim data (b, e, h) and COSMIC data (c, f, i) at 100 hPa (roughly 16 km, bottom), 50 hPa (roughly 21 km, middle), and 10 hPa (roughly 32 km, top) during the 2009 SSW event. The white curves in (a), (d) and (g) represent the dispersion relations of different wave components for different equivalent depth.

In 2009, the results of the equatorial band are shown in Fig. 4: the wavenumber-frequency spectra of the symmetric temperature perturbations using ERA-Interim data (Fig. 4a, d and g), the time–longitude cross section of Kelvin wave variances derived from ERA-Interim data (Fig. 4b, e, and h) and COSMIC data (Fig. 4c, f and i) at 100 hPa (roughly 16 km, bottom), 50 hPa (roughly 21 km, middle), and 10 hPa (roughly 32 km, top). The white curves in the Fig. 4a, d, and g represent the dispersion relations of different wave components for different equivalent depth. It is clear that Kelvin wave dominates the symmetric spectra in both the upper troposphere and stratosphere (Fig. 4a, d, and g). The spec-
tral peaks of Kelvin wave in the upper troposphere are constrained to \(8 \text{ m} < h < 90 \text{ m} \) \((9 \text{ m s}^{-1} < c_s < 30 \text{ m s}^{-1})\) while shift to higher frequencies and equivalent depths (i.e. phase speeds) in the stratosphere. This phenomenon could be explained by that Kelvin waves with higher frequencies and phase speeds could propagate to higher altitude more easily (Salby et al., 1984). Kelvin wave variances extracted by these two data sets are very similar both in the upper troposphere and stratosphere (Fig. 4b, e, and h and 4c, f, and i, respectively), which means that the result of ERA-Interim reanalysis data could reproduce most of the primary features of the realistic Kelvin waves.

### 4.2 Variation of Kelvin waves

#### 4.2.1 The 2009 event

In this section, we studied the variation of Kelvin waves during SSW events. Since zonal wind in the tropical region affects the propagation of the Kelvin waves, we first present the variation of zonal mean anomalous zonal wind in the 2009 event averaged between 10° S and 10° N (Fig. 5a). To illustrate the variations more clearly, we present both physical values (color shades) and the normalized values (black contours). It is obviously shown that the eastward anomalies (positive value) appeared in stratosphere within the SSW duration. The eastward anomalies larger than 1σ in the stratosphere first appeared around day −5 at 5 hPa and peaked around day −3. From the Eq. (1) described in Sect. 3.1, we know that the variation of zonal wind is affected by both Coriolis torque and the wave forcing. While in the tropical region (especially the equatorial region), the Coriolis force is too weak. Thus, the enhancements of westerly anomalies mentioned above are mainly caused by the tropical wave forcing. As the eastward propagating Kelvin waves are the dominant wave components in the tropical region, the Kelvin wave could contribute greatly to the enhancement of tropical eastward zonal wind anomalies.

Figure 5b depicts the temporal variation of Kelvin wave strength averaged between 10° S and 10° N from day −15 to day 15 in 2009. The strength of Kelvin wave is expressed as \(\frac{1}{2} T_{KW}^2\), where \(T_{KW}^2\) is the variance of Kelvin wave extracted from temperature field, overbar denotes zonal mean. Note that the physical values of Kelvin wave strength (color shades) are shown in non-detrended form while the normalized values are shown in detrended form to represent the significant enhancements (positive) or suppressions (negative). It is noticeable that enhancement of Kelvin wave appeared around day −8, when the tropical convection started to increase (see Fig. 2d), indicating that the Kelvin waves started to be activated due to the strengthened tropical convection. The Kelvin waves near 100 hPa were relatively strong during the whole SSW duration with two apparent peaks appearing around day −7 and day 4, respectively. Corresponding to the two peaks near 100 hPa, two peaks of Kelvin wave also appeared in the stratosphere above 20 hPa. An apparent suppression appeared above 30 hPa around day 0. Then, it arouses a question here regarding which factor, the variations of wave source or the wind filtering, contributes more to the Kelvin wave variability.

To elucidate the question above, we studied the longitudinal distribution of Kelvin wave strength and its relation with zonal wind and tropical convection. The definition of Kelvin wave strength here is the same with that mentioned above, but without zonal mean (i.e. \(\frac{1}{2} T_{KW}^2\)).

Figure 6 presents the time evolution of Kelvin wave strength (color shades), zonal wind (black contours), and OLR (black lines) during the 2009 SSW event. Before the SSW event (day −15, Fig. 6a), the Kelvin wave was relatively weak and the convection (low values of OLR) localized around the western Pacific (100–150° E). From day −15 to day 10, the total strength of the Kelvin waves became much stronger as the zonal mean convection started to enhance (see Figs. 2d and 5b), the convection in the western Pacific was intensified, and enhancement of Kelvin wave strength emerged in this region, corresponding to the convection peak (Fig. 6b). The correspondence between the peaks of Kelvin wave and convection in the western Pacific also occurred on day −5 (Fig. 6c).
Figure 6. The longitude-altitude cross sections of Kelvin wave strength (color shades), zonal wind (black contours), and the longitudinal series of OLR (black solid lines) at day $-15$ (a), $-10$ (b), $-5$ (c), 0 (d), 5 (e), 10 (f) of the 2009 SSW event. All the characters above are averaged between $10^\circ$S-$10^\circ$N. The solid contours indicate eastward wind and the dashed ones indicate the westward. Bold contours indicate the zero wind. The data are smoothed by a 5-day running mean. The dashed black lines indicate the zonal mean OLR averaged from day $-15$ to day 15.

On the central date of SSW event (day 0), the Kelvin wave strength became relatively weaker compared to day $-5$ because the convection around the western Pacific decayed. It is noticeable that the convection around South America (around $300^\circ$E) intensified, and the longitudinal distributions of the Indo-Pacific convection on the equator became more zonally symmetric. Yoshida and Yamazaki (2011) suggested that the zonal extension of tropical convection was linked to decrease of heating by vertical convergence of vertical heat flux in the tropical uppermost troposphere. It seems that the variation of Kelvin waves in Fig. 5b is more related with the localized convection of the Indo-Pacific region.

As we suggested that the tropical convection contributes more to the Kelvin wave activity during an SSW event, the results presented in Figs. 5b and 2d may seem to be controversial. It is noticeable that the enhancement of zonal mean Kelvin wave activity appeared around day $-10$ to day $-5$ (Fig. 5b), when the zonal mean convection was not that significant (zonal mean convection just started to increase, and OLR anomalies were still positive, Fig. 2d). But around day 0, when the peak of zonal mean convection appeared, the Kelvin wave became relatively weaker both around TTL and in the stratosphere. In fact, the enhancement of tropical convection first occurred around day $-10$ in the Indo-Pacific region (Fig. 6). Although the zonal mean convection was stronger around day 0 than what it was around day $-10$, the convection in the Indo-Pacific region decayed. Since the longitudinal distributions of Kelvin wave activity and OLR shown in Fig. 6 suggest that the Kelvin wave activity corresponds to localized Indo-Pacific convection, that is the reason of the correspondence between enactments of zonal mean Kelvin wave and zonal mean convection.

After the central day, the Kelvin wave strength enhanced around day 5 but with a westward shift of peak compared to that before day 0, corresponding to the convection enhancement of the western Pacific. When approaching the end of
the SSW duration, the longitudinal distribution of zonal wind filed and convection tended to recover to the pre-warming conditions.

4.2.2 The composite event

The composite analysis is also applied to investigate the temporal variation of tropical zonal wind and Kelvin waves (Fig. 7). Besides the physical values (color shades), we also plotted the Student $t$ value to represent the significant part.

The temporal variation of zonal mean anomalous zonal wind in the composite event averaged between 10° S and 10° N is shown in Fig. 7a. Significant zonal wind variation mainly occurred above 50 hPa. Enhanced eastward anomalies appeared from day −10 to day −3, corresponding to the enhancement of Kelvin wave (Fig. 7b). This phenomenon indicates that the enhancement of anomalous westerly zonal wind in the stratosphere is a common feature during SSW events, and the enhancement mainly occurs before the central date of SSW events. Our result is consistent with Chandran and Collins (2014).

The variation of Kelvin wave strength during the composite event is generally the same with that in the 2009. Kelvin wave in the upper troposphere was relatively strong all through the SSW duration. Two enhancements occurred in the stratosphere above 20 hPa, one showed up on day −8, while the other on day 11. The gaps between the two enhancements are relatively longer than those in the 2009 event, which are 10 days all through upper troposphere to stratosphere. Around day 0, significant suppression appeared above 50 hPa.

The results of longitudinal distribution of Kelvin wave, zonal wind anomalies, and OLR in the composite event are shown in Fig. 8. Note that only the Kelvin wave strength with confidence level higher than 95 % is shown. The wind field is composited by the anomalous value as departure from zonal mean and expressed in $t$ value because wind anomalies are more meaningful than zonal wind since the QBO phases during these SSW events were different. Similar to the 2009 event, localized convection lied within the Indo-Pacific region first intensified on day −10. While approaching day 0, the convection in the western Pacific decreased, and the longitudinal distributions OLR became more zonally symmetric. Alexander et al. (2008) once reported that the convective coupling with Kelvin waves was not always clear, while the correspondence between Kelvin waves and convection peaks in our results, especially near the TTL, suggested that Kelvin wave strongly coupled with tropical convection during SSW events. In the stratosphere above 100 hPa, where the Kelvin wave freely propagated (Alexander et al., 2008), strong Kelvin wave would be found near the zero wind lines, indicating that the upward propagation of the Kelvin waves is also affected by wind filtering.

As a summary, we know that the Kelvin waves coupled with localized Indo-Pacific convection during SSW events. Kelvin waves could interact with zonal wind in the stratosphere of the tropical region and contribute to driving the eastward zonal wind anomalies in the Indo-Pacific region above 30 hPa during SSW events. On the other hand, the vertical propagation of Kelvin wave is also affected by the zonal wind field through wind filtering.

5 Discussion

The previous sections present the variability of tropical background and Kelvin wave activities during SSW events, from which arose several questions.

The peaks of Kelvin wave activity in the stratosphere may seem to be strange as they do not always correspond to the eastward anomalies of zonal wind, but note that we presented the zonal wind anomalies instead of zonal wind in Figs. 5a and 6a. Taking the 2009 event for example, though the eastward anomalies of zonal wind appeared around day 0 in the stratosphere, the zonal mean zonal wind was easterly throughout the whole duration of the SSW event, which was a favorable condition for the propagation of Kelvin wave. So,
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Figure 8. The longitude-altitude cross sections of Kelvin wave strength (color shades) shown only those corresponding to the significance level higher than 95%, zonal wind (black contours), and the longitudinal series of OLR (black solid lines) at day −15 (a), −10 (b), −5 (c), 0 (d), 5 (e), 10 (f) of the composite SSW event. All the characters above are averaged between 10°S and 10°N. The solid contours indicate eastward wind anomalies and the dashed ones indicate the westward shown in t value. Bold contours indicate the zero wind. The data are smoothed by a 5-day running mean. The dashed black lines indicate the 95% significance level of the averaged OLR of the composite event.

the Kelvin wave in the stratosphere may not necessarily correspond to the eastward zonal wind anomalies.

In Sect. 4, we reported that Kelvin wave may contribute to driving the equatorial eastward anomalies of zonal wind during the SSW events, from which arose a question, i.e. to what extent would Kelvin wave contribute to the changes of zonal wind? To quantify the Kelvin waves forcing, we calculate the vertical gradient of the vertical flux of horizontal momentum, i.e.

\[ F_{KW} = \frac{\partial u'w'}{\partial z} \],

where \( u' \) and \( w' \) are the zonal wind and vertical velocity perturbations due to Kelvin waves retrieved from ERA-Interim reanalysis data, the overbar denotes the zonal averaging. The Kelvin wave signatures derived from the vertical velocity data, whose accuracy may be questionable due to the difficulty of detection, were compared with those derived from temperature field. The Kelvin wave signatures are clear in the vertical velocity field, and the frequencies are consistent with those in the temperature field (not shown). The relative contributions of Kelvin waves forcing are expressed as ratio with respect to the total zonal acceleration (i.e. \( F_{KW}/U_t \)). To avoid the abrupt transition caused by the sparse pressure levels when calculating \( F_{KW} \), the \( u'w' \) and zonal wind \( U \) obtained from the original pressure levels are interpolated by spline interpolation to [200], 190, [175], 162.5, [150], 137.5, [125], 112.5, [100], 90, 80, [70], 65, 60, [50], 45, 40, [30], 25, [20], 15, [10], 8, [7], 6, and [5] hPa (with vertical resolutions of 0.5 km below 50 hPa and 1 km above, roughly); the brackets represent the original pressure levels. Furthermore, a 3-day running mean is applied to smooth the interpolated data.

Figure 9 shows the altitude-time cross sections of the percentage of total zonal wind acceleration due to Kelvin wave forcing (color shades) calculated from ECMWF reanalysis data during 2009 SSW event (Fig. 9a) and the composite SSW event (Fig. 9b), the anomalous equatorial zonal wind (physical values presented in Figs. 5a and 7a) are over plotted. During the 2009 SSW event, peak Kelvin wave accelerations were generally observed when the westward anomalies (black dashed contours) started to decrease or when the eastward anomalies (black solid contours) started to increase. The Kelvin wave acceleration constituted between 5 and 30% of the total zonal wind acceleration in the stratosphere, while in the upper troposphere, that range turned into 10 and 60%. Two bulks of enhancement appeared at 20 hPa and right above 200 hPa around day 5, accordant to the en-
hancement of Kelvin waves (see Fig. 5b). The phenomena above confirmed that, Kelvin wave contributed prominently to the equatorial eastward zonal wind anomalies during the 2009 SSW event.

Similar pattern of Kelvin wave acceleration described above emerged in the composite event. In our study, we neglected the different QBO phases during the SSW events, which could also affect the Kelvin wave accelerations. Because the timescales of the variations of zonal wind and Kelvin wave strength during SSW events (generally within 1 month) are much shorter than QBO. The composited result showed that the Kelvin wave contribution was significant above 100 hPa and the averaged Kelvin wave contribution ranged from 5 to 35%. The result confirms that the Kelvin wave is one of the main contributors to the equatorial zonal wind changes during SSW events.

We also calculated the Kelvin wave acceleration during mid-winters without SSW events. Since it is impossible to define day 0 during winters without SSW, we chose several Januaries without SSW (1982, 1983, 1988, 1991, and 2011) to generally represent the non-SSW mid-winters. The averaged result is shown in Fig. 9c. Distribution of Kelvin wave acceleration shows clear differences between SSWs and non-SSWs. The Kelvin wave acceleration during SSWs mainly appears in the stratosphere above 30 hPa, while no significant Kelvin wave acceleration appears in that region during non-SSW winters, indicating the more important role of Kelvin wave in the zonal wind variability during SSWs.

Though Kelvin wave acceleration to eastward zonal wind anomalies is clear and significant during SSWs, however, the Kelvin wave forcing alone is insufficient in driving the equatorial eastward anomalies during SSWs, which suggests that the effects of other types of eastward propagating equatorial waves (e.g. eastward propagating gravity waves) excited by enhanced convection may not be neglected. In short, the mechanisms of the equatorial eastward zonal wind anomalies during SSW events are still complicated, further studies are needed to understand the related factors.

6 Conclusions

The tropical background changes as well as the spatial and temporal variability of Kelvin waves during SSW events are investigated by the ERA-Interim reanalysis data, and the results are validated by the COSMIC temperature data.

Our results support the idea that the tropical changes and the SSWs are two results due to the extratropical planetary wave forcing. The enhancement of extratropical planetary wave forcing causes the warming events in the polar region, also enhances the meridional circulation, and then in turn leads to the tropical upwelling. The tropical upwelling induced by the meridional circulation will further cause temperature decrease in the tropical stratosphere and upper tropo-
also affected by the zonal wind field during SSW events. Which suggests that vertical propagation of Kelvin waves was stronger during SSWs, but it is beyond the scope of this study. Moreover, resolution models, should be applied on the Indo-Pacific region in understanding the Kelvin wave variability during SSWs. The averaged contributions of Kelvin wave of all these events ranged from 5 to 35%, much larger than in the non-SSW mid-winters. However, averaged values suggest that the Kelvin wave forcing alone is insufficient in driving the equatorial eastward anomalies during the SSW events, and the contributions of other types of eastward propagating equatorial waves should be taken into account.

The longitudinal distribution of Kelvin wave, especially around the TTL layer, corresponded well to the localized Indo-Pacific convection, which suggests that Kelvin wave strongly coupled with localized tropical convection during SSW events. Ryu and Lee (2010) suggested that the TTL in the western tropical Pacific responded to the wave forcing more significantly than the eastern Pacific. It is also interesting that the significant eastward zonal wind anomalies in the stratosphere were mainly distributed within the Indo-Pacific region above 30hPa (Fig. 8). All these results indicate that more detailed future studies, including observation and high-resolution models, should be applied on the Indo-Pacific region in understanding the Kelvin wave variability during SSWs, but it is beyond the scope of this study. Moreover, strong Kelvin wave mainly located near the zero wind lines, which suggests that vertical propagation of Kelvin waves was also affected by the zonal wind field during SSW events.

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