Ion drift simulation of sudden appearance of sub-keV structured ions in the inner magnetosphere

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Abstract. Energy–latitude dispersed structured sub-keV ions in the inner magnetosphere often show significant development or intensification (by more than factor of 3) within 1–2 h near noon or afternoon where the azimuthal ion drift velocity at the sub-keV range is expected to be near zero. To examine whether such sudden appearances in the dayside can be explained by the drift motion of ions that are formed during substorm-related injections, we numerically simulated two such examples, one at noon and the other in the afternoon, based on the ion drift model. For both cases, the ion drift model with finite duration of proton source in the nightside can explain the observed large inbound–outbound differences in the sub-keV proton population without any new sources. Ion drift motion can thus cause rapid changes of complicated ion populations, at remote places from the source a long time after the substorm activities.

Keywords. Magnetospheric physics (energetic particles, trapped)

1 Introduction

Trapped hot ions at an energy range of 0.05–5 keV in the inner magnetosphere have complicated morphologies and mirror altitudes at different longitude, geomagnetic conditions, and L values (McIlwain, 1974; Quinn and McIlwain, 1979; Ejiri et al., 1980; Fennell et al., 1981; Sauvaud et al., 1981; Newell and Meng, 1986; Ebihara et al., 2001, 2004; Yamauchi et al., 1996, 2013). These trapped hot ions in the inner magnetosphere bounce between the Northern Hemisphere and the Southern Hemisphere with short bounce periods of only about 11 min for 100 eV protons and 4 min for 1 keV protons at L = 4 (see, e.g., Quinn and McIlwain, 1979). Therefore, the energy–latitude patterns of ion populations of > 100 eV in the inner magnetosphere are expected to be symmetric around the equator when the timescale is more than 0.5 h in this region.

Using this feature, Yamauchi et al. (2013) statistically examined the temporal evolution of three types of structured ions that are commonly found at sub- to few keV range in the inner magnetosphere using inbound–outbound differences in the proton data taken by the Cluster Ion Spectrometry (CIS) COMposition DIstribution Function (CODIF) instrument (Rème et al., 2001). Cluster orbits of perigee traversals in the inner magnetosphere during the 2001–2006 period are nearly symmetric about the equatorial plane along nearly the same longitude, with less than 1–2 h local time (LT) difference between the inbound and the outbound passes. The symmetry with respect to the equatorial plane for both the orbit and the motion of trapped ions allowed Yamauchi et al. (2013) to interpret the inbound–outbound differences in the latitudinal profile of the 0.1–1 keV ion population as temporal changes by, for example, ion energization, transport, or loss, with a timescale of the order of an hour. The three common types of structured ions examined in Yamauchi et al. (2013) are (1) wedge-like energy–latitude dispersed structured ions at sub- to a few keV, hereafter called as “wedge-like dispersed ions” (Yamauchi et al., 1996; Ebihara et al., 2001); (2) short-lived dispersionless ion stripes at wide energy range extending 0.1–10 keV (McIlwain, 1975; Yamauchi et al., 2006); and (3) short-lived low-energy ion bursts at less than a few hundred eV (Yamauchi et al., 1996). For all three ion populations at almost all local times,
traversals with significant enhancement (by more than factor of 3 in energy flux density) or asymmetry in the energy–latitude dispersion direction are more frequently observed than the symmetric cases.

The second category is mostly found in the midnight sector during substorms, and sudden enhancement or appearance within 1 h is not surprising if the phenomenon is directly driven by the substorm (Yamauchi et al., 2013). The third category is found at all local times and can be interpreted as local phenomena with a short timescale of no more than 1 h. On the other hand, the first category (wedge-like dispersed ions) is often observed in the morning-to-noon sectors, and represents the ion population that drifts more than a few hours after they are formed during substorms in the midnight-to-morning sectors (Ebihara et al., 2001; Yamauchi and Lundin, 2006; Yamauchi et al., 2009).

The inbound–outbound differences within 1–2 h for wedge-like dispersed ions can be understood if the observation is in the morning sector, because the eastward \( E \times B \) drift exceeds the westward magnetic drift significantly at sub- to few keV range, such that ions may drift significantly within 1–2 h, where \( E \) is the summation of co-rotation electric field and the externally imposed electric field. However, the inbound–outbound differences in the noon and afternoon sectors cannot be intuitively understood because the azimuthal component of the ion drift at sub-keV energy is expected to be very small near noon and in the afternoon.

Figure 1 shows two such examples of wedge-like dispersed ions observed by CODIF in spacecraft (SC) 4 during (a) 04:30–07:00 UT on 9 July 2001, and (b) 02:30–05:00 UT on 8 September 2002. The wedge-like dispersed ions are indicated by the black empty arrows. There are two types of asymmetry in this category: one with simple enhancement (or decay) in the intensity as shown in Fig. 1a (9 July 2001) and the other with asymmetric energy–latitude dispersion directions as shown in Fig. 1b (8 September 2002). Out of all clear events of the wedge-like dispersed ions observed during 2001–2006 by Cluster CIS/CODIF, the first type of asymmetry was observed 46 % of the time at 06–10 LT, 33 % of the time at 10–14 LT, and 35 % of the time at 14–18 LT respectively, and the second type of asymmetry was observed 30 % of the time at 06–10 LT, 23 % of the time at 10–14 LT, and 35 % of the time at 14–10 LT respectively (Yamauchi et al., 2009, Fig. 5).

The frequent occurrence of traversals with significant inbound–outbound differences in the wedge-like dispersed ions indicates either new injections or high eastward drift velocity even in the afternoon sector. For the drift velocity, Yamauchi and Lundin (2006) analyzed the Viking satellite data to show that the eastward ion drift could be much faster than the model, supporting the second possibility. However, a quantitative study such as the numerical simulation is needed to examine whether the drifting model alone can explain the enhancement within 1–2 h near local noon or if we need new sources to explain it (Yamauchi et al., 2013).

The purpose of this paper is to perform a particle drift simulation to answer this question. No past work simulated the wedge-like dispersed ions with inbound–outbound differences or asymmetries in the noon–afternoon sector. We use the same simulation model that was used in Yamauchi et al. (2009), which has successfully reproduced the ion pattern of an inbound–outbound symmetric event at 05 MLT observed by Cluster CIS/CODIF as a result of ion drift starting from low-energy (temperature is several tens of eV) ions at the nightside 8 Earth radii (\( R_E \)) boundary. Two examples shown in Fig. 1 are simulated: (a) SC-4 during 04:30–07:00 UT on 9 July 2001 and (b) SC-4 during 02:30–05:00 UT on 8 September 2002. Since oxygen ions and protons are different in Fig. 1, we simulate only protons in this paper.

## 2 Simulation method

The numerical model used in Yamauchi et al. (2009) (originally from Ebihara et al. (2001, 2008)) calculates the ion drift motion in the inner magnetosphere for both the energy-dependent magnetic (gradient-B and curvature) drift and the energy-independent \( E \times B \) drift. The details of the numerical scheme are described in Ebihara et al. (2008). For magnetic and external electric fields, a dipole magnetic field and the Weimer-2001 type convection electric field model (Weimer, 2001) are employed with the solar wind parameters obtained from the 5 min resolution NASA/OMNI data set. Such a simple magnetic field is sufficient for the present purpose because we do not focus on the exact reconstruction of the source proton distribution. According to previous simulation works (e.g., Angelopoulos et al., 2002; Ebihara et al., 2004), the Weimer model gives a better explanation for the motion of ions in the inner magnetosphere than the Volland–Stern type model (Volland, 1973; Stern, 1975) does. For the particle loss, we assumed charge exchange decay in the same way as Ebihara et al. (2001).

The actual calculation is performed in two steps: (a) we first trace the observed proton distribution backward using the phase-space mapping method (e.g., Kistler et al., 1999; Ebihara et al., 2008); (b) we then perform a forward drift simulation assuming a boundary condition that is estimated from the back-tracing result. The backward tracing is necessary to estimate a proper boundary condition. Since one phase-space point in the observation is mapped to only one phase-space point by the Liouville theory, the backward tracing can cover only limited areas in location and energy for a given time.

Therefore, we need some assumption to estimate the proton distribution function at the starting boundary for the drifting protons (we take it at 8 \( R_E \)) that is consistent with the backward tracing result. Here, we assume a single phase-space density distribution across the entire 8 \( R_E \) boundary, and we interpolate the backward tracing result into a simple proton distribution function that is common at all points.
along the boundary for one time. The backward tracing is stopped when either protons reach the 8 $R_E$ boundary or backward elapsed time exceeds a certain time (34 h in the present case).

For both examples in Fig. 1, the backward tracing result predicts a low-energy source distribution at 8 $R_E$ boundary with proton density about 0.5 cm$^{-3}$ and proton temperature about 50 eV, and mainly in the nightside for a limited time interval. Such low-energy sources are already predicted in Ebihara et al. (2008) and Yamauchi et al. (2009), in which the simulations are compared with the observations. The predicted low-energy proton distribution is also consistent with the cold ion supply from the ionosphere to the plasma sheet through the tail lobe (Engwall et al., 2009), in which the ion flow was obtained in the lobe region because of the low density, but without solid information of exact temperature.

For the forward simulation, the reconstructed proton distribution at 8 $R_E$ is used as the boundary condition for both examples in Fig. 1. A limited time interval is mandatory to reproduce striping structure instead of filled structure in the spectrogram (Ebihara et al., 2001). The detailed scheme of the forward simulation including the assumed decay rate is described in Ebihara et al. (2004).

### 3 Numerical result

#### 3.1 The 9 July 2001 event

The wedge-like dispersed ions (black empty arrows) in Fig. 1a are intensified more during the outbound (05:50–06:50 UT) than during the inbound (04:50–05:50 UT) at 15–16 MLT. Almost no signature is seen in the oxygen data for this signature, probably due to low counting rate of the oxygen ions. Figure 2 shows 5 min averaged OMNI solar wind parameters and auroral electrojet upper (AU) and lower (AL) indices for this event. The constant solar wind velocity (~ 450 km s$^{-1}$) and gradual change of the interplanetary magnetic field (IMF) northward component (from $B_z$ ~ $-5$ nT to ~ $+3$ nT) during the past 10 h caused a monotonic drop of geomagnetic activity from its peak (AL ~ $-700$ nT) at around 02:30 UT to a quiet level (AL ~ $-30$ nT) after 06:10 UT.

Figure 3 shows the numerical simulation result of the proton differential energy flux with local pitch angle of 90° at the location of observed latitude by the Cluster SC-4. The observed ions have pitch angles less than 90°, but without solid information of exact temperature.

However, the eastward drift velocities of the protons with smaller equatorial pitch angles than the observed ones are only slightly faster than the observed protons, even after considering the difference in the drift velocity at different pitch angles for the competing magnetic drift (Ejiri, 1978; Yamauchi et al., 2006). It is possible to tune the pitch angle distribution to match the observation, but adding such a “free parameter” defocuses the most important mechanisms that cause the general asymmetric feature.

These protons are assumed to start at the outer boundary at 8 $R_E$ in the nightside during a limited time interval from 10:00 UT to 13:00 UT, with a density of 0.5 cm$^{-3}$ and temperature of 50 eV. This boundary condition is selected based on the backward tracing result of the observed protons. The supply timing is not necessarily the same as the substorm onset because these cold ions come from the ionosphere as a result of the substorm activity. With this boundary condition,

![Fig. 1. Energy–time spectrograms of 4-pi averaged proton (H+, upper) and oxygen ion (O+, lower) differential energy fluxes observed by Cluster spacecraft-4 CIS/CODIF at 0.1–40 keV during (a) 04:50–07:00 UT on 9 July 2001, and (b) 02:30–05:00 UT on 8 September 2002. The black empty arrows indicate the energy–latitude dispersed structure sub-keV ions that are simulated in this paper, and red empty arrows indicate mono-energetic keV ions that are discussed in Yamauchi et al. (2009).](image-url)
we reduced the Weimer-2001 electric field by half in the dayside to reproduce the result shown in Fig. 3.

Figure 3a shows the virtual spectrogram using the simulated proton data assuming the Cluster SC-4 traversal. The simulation predicts the enhancement of the sub-keV population in a limited energy range during the outbound traversal only and not during the inbound. This asymmetry is similar to that shown in Fig. 1a. Figure 3b shows the elapsed time of observed protons from the start location that is located at 8 \( R_E \) on the nightside. The elapsed time is calculated from the backward particle tracing from the observed space–time, and, therefore, the figure contains even high-energy ions that are not simulated in the forward method. Because the convection is time-varying, the calculated elapsed time is shorter for the enhanced sub-keV protons during the outbound (about 15 h) than for virtual sub-keV protons that would have appeared at the timing of inbound. In this way, the Cluster SC-4 traversed the inbound pass before the protons reached the satellite location. This is more clearly illustrated in Fig. 3c.

Figure 3c snapshots the differential flux of protons with energy of 0.1 keV with equatorial pitch angle of 90°. During the inbound traversal, the 0.1 keV proton stripe did not reach the spacecraft location, while it passed the spacecraft location at the time of the outbound traversal. Thus, the spacecraft can observe significant development of the low-energy population within 1–2 h.
3.2 The 8 September 2002 event

A similar intensification of the wedge-like dispersed ions (black empty arrows) as the previous event is also found in Fig. 1b from the inbound (03:00–04:00 UT) to the outbound (04:00–05:00 UT) at around local noon. In addition, the energy–latitude dispersion directions of the wedge-like dispersed ions are opposite (i.e., the same energy–time dispersion direction) between the inbound and the outbound. Overlapping to these wedge-like dispersed ions, an intensified ion band at around 1–3 keV is also observed as indicated by the red empty arrows. This ion band is outstanding in the oxygen data, and thus the O / H ratio is quite different between the wedge-like dispersed ions and the ion band.

Figure 4 shows 5 min averaged OMNI solar wind parameters and AU and AL indices for this event. After the coronal mass ejection (CME) hit the Earth at around 17:00 UT (about 11 h before the traversal), the solar wind velocity gradually decreased from a high value of 550 km s$^{-1}$ to about 480 km s$^{-1}$ at the time of the Cluster traversal. During the same period, the IMF was very intense (about 20 nT total field) with a large southward component ($B_z \sim -10$ nT) from even before the CME arrival until just before the Cluster traversal, causing very high geomagnetic activities of continuously $AL < -500$ nT with many substorm onsets, at around 16:40 UT, 18:30 UT, 22:50 UT, 01:20 UT and 05:10 UT.

Figure 5 shows the numerical simulation result in the same format as Fig. 3. For this simulation, protons are assumed to depart at the nightside outer boundary of 8 $R_E$ during two intervals: 20:00–21:00 UT and 22:00–23:00 UT, with a density of 0.5 cm$^{-3}$ and temperature of 50 eV, based on the backward tracing result of the observed protons. Figure 5a reproduced two essential features of Fig. 1b: enhancement of the sub-keV ion population in the outbound, and the asymmetric energy–latitude dispersions with respect to the equator (increasing energy with time in both the inbound and outbound).

In addition, the simulation also reproduced the ion band at around 1–3 keV. This ion band has a different start time from the wedge-like dispersed ions, as shown in Fig. 5b. Therefore, the different O/H ratio between the wedge-like...
dispersed ions and the band-like ions can be explained as different O/H ratios at different UTs at the outer boundary of 8 $R_E$. Since both the magnetic and $E \times B$ drifts are mass independent when comparing ions with the same energy (Roederer, 1970, page 57; Yamauchi et al., 2006, Eq. 3), drift motion cannot filter out different ion species to explain the observed O/H difference.

Figure 5b also shows that the elapsed time for the outbound sub-keV signature to reach the Cluster location is shorter than the virtual inbound sub-keV ions would have taken to reach the Cluster location. According to Fig. 5c, the last (westward-most) stripe of 0.1 keV proton has not reached the spacecraft location during the inbound traversal, while it passed the spacecraft location at the time of the outbound traversal. Thus, the spacecraft can observe significant development of the low-energy ion population within 1–2 h in this example too.

4 Discussion

We have simulated two examples at 15–16 MLT and 12 MLT, respectively, where the eastward ion drift normally slows down or even stagnates at the 0.1–1 keV energy range. The general features of the sub-keV ions are well reproduced even with the present simplified simulation settings, and the shape of the simulated wedge-like structure resembles those that are observed. In other words, the eastward drift is sufficiently fast to cause the inbound–outbound difference in the early afternoon sector when viewed by the Cluster satellite. Since the eastward drift is faster in the morning sector than the noon–afternoon sectors, we expect a higher degree of asymmetry there, as has previously been observed (Yamauchi et al., 2013).

During highly disturbed conditions, the induction electric field becomes dominant in the inner magnetosphere (e.g., Ohtani et al., 2010), and the modeling of the induction electric field is problematic. A stronger electric field than the ideal model field is also suggested from statistics of the wedge-like dispersed ions from Viking (Yamauchi and Lundin, 2006) and Cluster (Yamauchi et al., 2006). In such a case, the eastward drift velocity will be enhanced, making the energy–time and energy–latitude dispersions stronger (i.e., more curved in the spectrogram).

Here we assumed the source location (where ions do not have dispersion) at 8 $R_E$ in the nightside, but the actual source location can be different, for example, in the late morning sector (Yamauchi et al., 2006) or even the near noon via direct supply from the ionosphere (Giang et al., 2009). Such an eastward shift of the source location shortens the eastward drift distance from the source to the spacecraft that traverses noon–afternoon sectors, making the elapsed time shorter and the energy–latitude dispersion weaker. Combining the stronger electric field than the model and closer distance of the source location, the elapsed time can be shortened while keeping the same strength of the energy–time dispersion. Therefore, the success of the present simulation with the 8 $R_E$ source in the nightside does not necessarily exclude the possibility of other source locations.

Considering various source locations is particularly important in interpreting different populations. For example, in the second event (8 September 2002), the simulation reproduced the band-like ions at 1–3 keV as originating at a different start time than the sub-keV dispersed ions (Fig. 5b). This means that their source locations are not necessarily the same: the band-like keV ion may have traveled a longer distance (e.g., from the plasma sheet) than the sub-keV dispersed ions (e.g., from morning). The clear difference in the O/H ratio between the two populations (Fig. 1b) supports this scenario.

There are many minor differences between the observation and simulation if one compares them in detail. For example, the peak of the differential energy flux in the first event is found at much lower energy (30 eV) in the observation (Fig. 1a) than in the simulation (about 300 eV). This indicates that the observed population can be a summation of two different sources: one the wedge-like dispersed ions that are simulated here, and the other the low-energy ion bursts (Yamauchi et al., 2013) that are also found in the inbound. Similarly, the peak flux problem is also seen in the inbound of the second event (1 keV in the observation in Fig. 1b and 200 eV in the simulation in Fig. 5a) and the central part (shape of peak differential energy flux is layer-like in Fig. 1b and rounded in Fig. 5a).

However, these details are rather a tuning problem using many realistic parameters, and such a discussion will miss the main point: the inbound–outbound differences and/or asymmetries of the sub-keV ions in the noon–afternoon sector can be reproduced by drifting ions coming from the nightside. The modifications of the electric field or source location would not alter the main result of reproducing the inbound–outbound difference and/or asymmetry. One-hour difference can certainly mean a large change in the observation at a fixed magnetic local time. The exact timing and location that such an inbound–outbound difference can be observed in the virtual spacecraft depends on these external parameters. In the present case, we had to reduce the Weimer-2001 electric field by half to reproduce the observed spectrogram. This in turn provides a good test on the electric field model.

5 Conclusions

We have simulated drifting low-energy ions in the inner magnetosphere to examine whether ion drift can explain the sudden appearance of energy–latitude dispersed structured sub-keV ions that are often observed during Cluster perigee traversals as inbound–outbound differences. We simulated two examples: one in the afternoon and the other near the noon. Both simulations showed that the sudden appearance of these low-energy ions can be explained by the drift motion.
only. Furthermore, the second simulation also succeeded in reproducing the asymmetric energy–latitude dispersion of this population as well as band-like ions at around 1–3 keV. The simulation indicates that the eastward azimuthal ion drift is fast enough to make significant changes in the inner magnetospheric sub-keV ion population within 1–2 h even in the noon–afternoon sector where the azimuthal ion drift is expected to nearly stagnate.

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