Ion cyclotron waves during the Rosetta approach phase: a magnetic estimate of cometary outgassing

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Abstract. A theoretical model for the ion cyclotron wave generation during the approach phase of Rosetta to 67P/Churyumov–Gerasimenko is presented. For various activity levels of the comet, the crossing of the observational threshold is determined, whose level is derived from the wave power in the undisturbed solar wind near the comet’s location during the approach phase at the appropriate frequency. The Giotto flyby at 27P/Grigg–Skjellerup is used to obtain an estimate of how often water-group ion cyclotron waves are observed, and to get insight into the wave forms. At 67P/Churyumov–Gerasimenko one can expect to observe water-group ion cyclotron waves already at a distance of 600 000 km from the nucleus for a nominal outgassing rate of \( Q = 350 \times 10^{23} \) molecules per second. The observed first location of cyclotron waves during the Rosetta approach phase will give an indication of the actual outgassing rate of the comet.

Keywords. Interplanetary physics (MHD waves and turbulence) – space plasma physics (waves and instabilities)

1 Introduction

After its wake-up call on 20 January 2014, the Rosetta spacecraft (Glassmeier et al., 2007a) will fly to its rendezvous with comet 67P/Churyumov–Gerasimenko (CG), where it will arrive on 6 August 2014, when the approach phase switches to the surface mapping phase of the mission. At the time of the arrival, the actual gas production of the comet is only roughly known. The observations during the last years (e.g. Schulz et al., 2004) and Weiler et al. (2004) or most recently Snodgrass et al. (2013)) predict at 3.5 AU (20 August 2014) a total gas production rate of \( 2.1 \times 10^{25} \) (low-activity case, LAC), \( 3.5 \times 10^{25} \) (Snodgrass et al., 2013) or \( 3.8 \times 10^{26} \) molecules s\(^{-1} \) (high-activity case, HAC). However, the actual gas production rate is an important quantity in the mission planning. As reported by Snodgrass et al. (2013), the comet started its activity in the 2007/2008 at a heliocentric distance of \( \sim 4.3 \) AU, and the authors predict a similar behaviour in 2014. Therefore, it is proposed to use the magnetometer of the Rosetta Plasma Consortium (RPC, Glassmeier et al., 2007b) to study to presence of ion cyclotron waves generated by freshly picked-up ions along the approach phase of Rosetta, concentrating on the last \( 2 \times 10^{06} \) km. These measurements can provide an estimate for the gas production rate of CG early in the approach phase.

2 Cometary outgassing and ion pickup

As a comet moves towards the Sun and comes closer than the orbit of Jupiter, the solar radiation is strong enough to warm up the nucleus and to make it start outgassing. To describe the outgassing with a rate \( Q \) [molecules s\(^{-1} \)], a spherical expansion of the gas cloud at speed \( V_e \) is assumed, and an ionization rate \( \nu \) [s\(^{-1} \)] is used for the loss through ionization. The number density \( N_c(r) \) of the gas cloud is then obtained as a function of radial distance \( r \) from the nucleus, taking the loss through ionization into account:

\[
N_c(r) = \frac{Q}{4\pi V_e r^2} \exp \left\{ -\frac{\nu r}{V_e} \right\}. \tag{1}
\]

Following Huddleston et al. (1990) all distances are scaled by \( L = V_e/\nu \), and the number of implanted ions per second into the solar wind is given by \( N_c(r)\nu \), giving rise to a total implanted particle flux \( n_i u_i \) (with \( n_i \) and \( u_i \) the ion density and velocity respectively) at a specific location \( r_0 \) along the...
solar wind flow (taken to be along the x direction):

\[ n_i u_i = \frac{Q}{4\pi L^2} \int_{x_0} \exp \left\{ -(x^2 + y_0^2 + z_0^2) \right\} \frac{1}{x^2 + y_0^2 + z_0^2} \, dx. \]  

(2)

The mass loading by the picked-up ions will slow down the solar wind. In order to calculate this effect, Huddleston et al. (1990) calculated the solar wind speed from a solution of the one-dimensional magnetohydrodynamic (MHD) equations (see also Biermann et al., 1967) for a gas with two degrees of freedom \( (f = 2) \). However, Koenders et al. (2013) showed that the interaction of the outgassing comet with the incoming solar wind is better described by a gas with three degrees of freedom \( (f = 3) \). The continuity equations (see Koenders et al., 2013) for the flow to have be fulfilled:

\[ \frac{\partial}{\partial x} (nu_s) = M_s, \]  

(3)

\[ \frac{\partial}{\partial x} \left( nu_s^2 + p_s \right) = I_s, \]  

(4)

\[ \frac{\partial}{\partial x} \left( \frac{1}{2} nu_s^2 + \frac{(f + 2)}{2} p_i u_s \right) = E_s, \]  

(5)

where \( n \) is the gas density, \( u \) the gas flow velocity and \( p \) the thermal pressure. \( M_s, I_s \) and \( E_s \) are the local density, momentum and energy sources. Biermann et al. (1967) showed that, of these, only \( M_s \) needs to be treated as non-zero, as long as the distance to the nucleus is much larger than stand-off distance of the ionopause of the comet. Therefore \( I_s = E_s = 0 \) is assumed, and integrating Eqs. (4) and (5) from \( -\infty \) to \( x_0 \), with the assumption that \( p_s = 0 \) and some basic algebra, setting \( f = 3 \) changes Eq. (13) in Huddleston et al. (1990)

\[ \frac{u_\infty}{u_{sw}} = 2 - \sqrt{4 - 3 \left( 1 + \frac{n_i u_i m_i}{n_{sw} u_{sw} m_{sw}} \right)}. \]  

(6)

to this version:

\[ \frac{u_\infty}{u_{sw}} = \frac{5}{2} - \sqrt{\left( \frac{5}{2} \right)^2 - 4 \left( 1 + \frac{n_i u_i m_i}{n_{sw} u_{sw} m_{sw}} \right)} \]  

(7)

where \( u_\infty \) is the undisturbed solar wind speed, \( u_{sw} \) the local (mass-loaded) solar wind speed and \( n_{sw} \) the mass-loaded solar wind density, and the pickup flux \( n_i u_i \) is obtained from Eq. (2).

From Eqs. (2) and (7) the pickup density and local (mass-loaded) solar wind speed can be obtained along the orbit of Rosetta, which is shown in Fig. 1 in cometarycentric solar equatorial (CSEQ) coordinates, where the x axis points towards the Sun, the z axis is aligned with the solar rotational axis and the y axis completes the triad.

The integral in Eq. (2) is numerically integrated, using the following parameters: \( v = 10^{-6} \) \( \text{m s}^{-1} \), \( V_0 = 1 \) \( \text{km s}^{-1} \), and undisturbed solar wind conditions with \( u_\infty = 380 \) \( \text{km s}^{-1} \), \( n_\infty = 0.9 \times 10^6 \) \( \text{m}^{-3} \), \( B_0 = 1 \) \( \text{nT} \) and the average solar wind ion mass \( m_{sw, \infty} = 1.2 \) \( \text{AMU} \).

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**Fig. 1.** The approach phase of Rosetta for the last \( 2 \times 10^6 \) km in CSEQ coordinates. Asterisks indicate the respective date and radial distance from the nucleus.

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**Fig. 2.** Top left: the ion pickup density along the orbit of Rosetta for various outgassing rates 50 (black), 350 (red), 650 (green) and 1000 (blue) \( 10^{23} \) \( \text{s}^{-1} \). Top right: the mass-loaded flow velocity \( u_{sw} \) in units of \( u_\infty \). Bottom left: the energy in the pickup ring distribution. Bottom right: the amplitude of the ion cyclotron waves assuming full scattering of the ring distribution. The dashed horizontal line at 0.1 nT indicates the solar wind noise level. The upper dashed line marks the 0.5 nT amplitude.

As the solar wind is not slowed significantly by the ion pickup during the approach phase, it is assumed under the square root of Eq. (7) that \( u_{sw} = u_\infty \) and \( u_{sw} = u_\infty \). The obtained \( u_{sw} \) at each point along the integration path is then used as \( u_i \) in the following step.

As the actual outgassing rate of CG is not known, a range of values for \( Q \) has been used: 50, 350, 650 and 1000 \( 10^{23} \) \( \text{s}^{-1} \), where the middle values are compatible with the prediction model of Snodgrass et al. (2013) closer to the Sun. A nominal rate of \( Q = 350 \times 10^{23} \) \( \text{s}^{-1} \) will be used as a base and agrees reasonably with the estimate of Snodgrass et al. (2013) with CG near 3.5 AU during the approach phase. The results for the pickup density and the mass-loaded solar wind speed are shown in Fig. 2 top left and top right panels.
In the assumption of a perpendicular magnetic field (i.e. $\mathbf{B}_{\text{IMF}} \perp \mathbf{v}_{\text{sw}}$), the freshly picked-up ions form a ring distribution, which is unstable for the generation of ion cyclotron (IC) waves (Lee, 1989; Gary, 1991) through scattering from a ring to a bi-spherical shell distribution (e.g. Huddleston and Johnstone, 1992). The total energy density in the ring distribution can be estimated as

$$E_{\text{ring}} = 0.5n_i m_i u_{\text{sw}}^2,$$

where $m_i$ is the ion mass, and the values for $n_i$ and $u_{\text{sw}}$ are taken from the calculation with Eq. (7) and shown in Fig. 2 top left and right panels. Assuming that all the energy of the ring distribution can be converted to IC wave energy, the amplitude of the waves can be estimated by

$$B_{\text{wave}} = \sqrt{2\mu_0 E_{\text{ring}}}. \quad (9)$$

The results of these two estimates are shown in Fig. 2 bottom left and right panels, respectively. The wave amplitude plot shows that for complete scattering and a moderate source rate of $Q = 350 \times 10^3 \text{ s}^{-1}$, the 0.1 nT waves may be expected already at $\sim 10^6 \text{ km}$ distance from the nucleus (lower dashed line). Unfortunately, the assumption of complete scattering is not valid and needs to be corrected.

Coates et al. (1989) defined an average age $\tau_i$ of the implanted ions picked up upstream and seen at the spacecraft at location $x_0$ in the solar wind flow for an outgassing comet:

$$\tau_i = \frac{L}{u_{\text{sw}}} \int_{x_0}^{\infty} \frac{\exp\left(-\left(x-x_0\right)^2+y_0^2+z_0^2\right)^{1/2}}{x^2+y_0^2+z_0^2} \, dx,$$

where, as above, the solar wind flow is assumed to be along the $x$ axis. This age of the ions should be compared to the scattering time $\tau_s$ of the ions from a ring distribution to a shell distribution, which was found to be four times the gyro-period in the wave field (Gaffey et al., 1988; Coates et al., 1989):

$$\tau_s = \frac{4}{\Omega_i} \left(\frac{\Delta B}{B_0}\right)^{-1}, \quad (11)$$

where $\Omega_i$ is the gyro-frequency in the background field $B_0$ and $\Delta B$ is the wave field. Note that, because of the little pickup expected (because of the low outgassing rate) and thus the little slowdown of the solar wind, the interplanetary magnetic field field strength, $B_0$, is kept constant in these calculations. It is clear from Fig. 3 top left panel that the age $\tau_i$ of the implanted ions (thick magenta line) is much lower than the scattering time $\tau_s$ (thin lines). This means that the ring distribution could have been fully scattered into a shell distribution, and thus the wave amplitude in Fig. 2 bottom right is an overestimation. In order to take into account the discrepancy between age and scatter time, the scattered energy is assumed to be

$$E_{\text{scat}} = \frac{\tau_i}{\tau_s} E_{\text{ring}}. \quad (12)$$

The results of this correction are shown in Fig. 3 top right panel, where it is found that 0.1 nT amplitude waves can be expected within the last $\sim 4 \times 10^6 \text{ km}$ from the nucleus for an outgassing rate of $Q = 350 \times 10^3 \text{ s}^{-1}$.

All calculations, up to now, have assumed that the ionization rate is constant at $\nu = 10^{-6} \text{ s}^{-1}$. Figure 3 bottom left panel shows the corrected wave amplitude for an outgassing source rate of $Q = 350 \times 10^3 \text{ s}^{-1}$ and an ionization rate $\nu$ varying between $10^{-6}$ and $10^{-8} \text{ s}^{-1}$.

### 3 Solar wind and Comet 27P/Grigg–Skjellerup

The above theoretical calculations will probably contrast with the data from a real encounter with a comet. Therefore, the magnetometer data from the Giotto flyby of comet 27P/Grigg–Skjellerup (GS) are studied for IC waves (e.g. see Neubauer et al., 1993; Glassmeier and Neubauer, 1993; Coates et al., 1993). Naturally, there are great differences between the CG approach phase and the GS flyby: GS was much closer to the Sun, had a stronger outgassing rate of $Q = 7 \times 10^2 \text{ s}^{-1}$ and had a fully developed bow shock. For CG a rate of $Q \leq 10^2 \text{ s}^{-1}$ is expected, and there will, most likely, only be a bow shock close to perihelion (Koenders et al., 2013). However, the situation upstream of a bow shock or Mach cone should not be affected by regions downstream. Thus in order to study the “homogeneity” of the ion pickup and IC wave generation in the upstream region of a comet, these data can be used.
The magnetometer data are transformed to a mean-field-aligned (MFA) coordinate system, where the mean field is determined using a low-pass filter for periods above 30 min, which represents the $Z_{MFA}$ direction, and the $X_{MFA}$ and $Y_{MFA}$ directions are chosen perpendicular to this direction. The transverse components $X_{MFA}$ and $Y_{MFA}$ are combined into a left- and right-hand polarized components. Ion cyclotron waves are left-hand polarized waves at or below the local cyclotron frequency in the spacecraft frame (Gary, 1991). A dynamic spectrum is produced with spectral analysis (McPherron et al., 1972) on sliding windows of 256 s with a shift of 64 s. The result for the left-hand polarized magnetic field component is shown in Fig. 4 top left panel, where the $x$ axis is time during the flyby, with closest approach at hour 39.25, where hour 0 is taken at 9 July 1992, DOY 191, at 00:00 UT, the inbound bow shock crossing was at hour 36.8 and the outbound at hour 41.3. Figure 4 top right panel shows the ellipticity for the frequency estimates, where negative ellipticity means left-hand polarized waves. The white over-plotted line in the panels marks the local $H_2O^+$ cyclotron frequency.

The cyclotron waves are identified for frequencies $0.8–1 f_{ci}$, which have either a ratio of left-hand over right-hand power $R > 1.5$ (e.g. see Delva et al., 2008) or an ellipticity $E < 0$. In the interval shown in Fig. 4 and Giotto within 500 000 km from the nucleus, there are a total of 1096 spectra of which 441 have $R > 1.5$ and 474 have $E < 0$, with the stronger restriction $R$ contained in the weaker $E$. This means that only $\sim 40 \%$ of the time during the flyby, IC waves were observed at GS. Two examples of IC wave intervals are shown in Fig. 4: bottom left the data for hour 34–35 (before closest approach and upstream of the bow shock), where there are irregular waves at the cyclotron frequency ($f_{ci} \approx 13 \text{ mHz}$); bottom right the data for hour 40–41 (after closest approach and downstream of the bow shock), where the waves look “anharmonic” (Glassmeier et al., 1997) at the cyclotron frequency ($f_{ci} \approx 17 \text{ mHz}$), but they are much better developed than in the earlier interval. Interestingly, calculating the ratio of the average age of the implanted ions and the scattering time reveals values of 4.3 and 4.5 for both intervals respectively. This means that, although the waves have had ample time to grow in both intervals, only the post-closest approach interval has well-developed, albeit “anharmonic” waves. This could indicate a difference in wave growth in the unshocked (first interval) and shocked solar wind plasma (second interval).
In order to find the minimal power level that the cyclotron waves need to achieve to be visible over the solar wind background noise, the magnetometer data from Pioneer 10 during its approach of Jupiter are studied at a radial distance from the Sun comparable to Rosetta’s approach to CG. The data and the power spectrum are shown in Fig. 5. At the local IC frequency \( f_{ci} \approx 0.8 \text{mHz} \), the wave power is \( \sim 1.9 \text{nT}^{-2} \text{Hz}^{-1} \), which corresponds to a wave amplitude of 0.1 nT. This gives an indication of the spectral power density that might be expected during the approach phase and of the cyclotron wave amplitudes that can be observed unambiguously by the Rosetta Plasma Consortium instruments.

4 Expectations for the approach phase

A theoretical model for the IC wave production along the approach of Rosetta to CG has been presented in order to make an early estimate of the activity level of the comet from the magnetometer data. In combination with data from the Giotto flyby of GS and solar wind data from Pioneer 10 near Jupiter, the following conclusions can be made:

- the solar wind noise level at the water cyclotron frequency is \( \sim 0.1 \text{nT} \), which sets a lower limit to the amplitude of the observable IC waves;

- depending on the outgassing rate, the waves cross the 0.1 nT threshold between 6 and \( 3.5 \times 10^5 \) km distance from CG for a source rate \( 1000 \times 10^{23} \geq Q \geq 350 \times 10^{23} \text{ s}^{-1} \);

- lower outgassing rates than the nominal value used in this paper will further reduce the radial distance at which IC waves may be observable;

- the spacecraft approach from \( 6 \times 10^4 \) km to closest distance takes place during 24 days of the mission. Based on observations at GS, IC waves are expected to be observable 40% of the time, which would give an accumulated 10 days of IC wave observation;

- because of the young age of the ions, the wave form might not be well developed;

- shocked and unshocked solar wind may have influence on wave growth and form; however, Rosetta will most likely not encounter a bow shock during its approach phase.

Although in the beginning of the outgassing of CG the sublimation of CO\(_2\) will dominate that of H\(_2\)O by a factor \( \sim 5 \) (see Snodgrass et al., 2013, Table 6), this paper concentrated on water group ions because of the much heavier molecular mass of carbon dioxide (44 vs. 18 AMU). The heavier mass lowers the cyclotron frequency by a factor 2.5: \( f_{\text{H}_2\text{O}} \approx 0.85 \) and \( f_{\text{CO}_2} \approx 0.35 \text{mHz} \), which makes the heavier ions more difficult to detect at low amplitude because of the long time segments of relatively constant solar wind conditions needed (e.g. see Delva et al., 2011, for a discussion of IC waves at Venus for varying solar wind cone angle).

In the middle of 2014, when the magnetometer data from the Rosetta approach phase will have arrived on Earth, an actual estimate of the outgassing rate of the comet can be made from the H\(_2\)O\(^+\) IC wave observations.

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