Meteor head echo polarization at 930 MHz studied with the EISCAT UHF HPLA radar

G. Wannberg¹, A. Westman², and A. Pellinen-Wannberg¹,³

¹Swedish Institute of Space Physics, P.O. Box 812, 98128 Kiruna, Sweden
²EISCAT Scientific Association, P.O. Box 812, 98128 Kiruna, Sweden
³Umeå University, 90187 Umeå, Sweden

Abstract. The polarization characteristics of 930-MHz meteor head echoes have been studied for the first time, using data obtained in a series of radar measurements carried out with the tristatic EISCAT UHF high power, large aperture (HPLA) radar system in October 2009. An analysis of 44 tri-static head echo events shows that the polarization of the echo signal recorded by the Kiruna receiver often fluctuates strongly on time scales of tens of microseconds, illustrating that the scattering process is essentially stochastic. On longer timescales (> milliseconds), more than 90 % of the recorded events show an average polarization signature that is independent of meteor direction of arrival and echo strength and equal to that of an incoherent-scatter return from underdense plasma filling the tristatic observation volume. This shows that the head echo plasma targets scatter isotropically, which in turn implies that they are much smaller than the 33-cm wavelength and close to spherically symmetric, in very good agreement with results from a previous EISCAT UHF study of the head echo RCS/meteor angle-of-incidence relationship.

Significant polarization is present in only three events with unique target trajectories. These all show a larger effective target cross section transverse to the trajectory than parallel to it. We propose that the observed polarization may be a signature of a transverse charge separation plasma resonance in the region immediately behind the meteor head, similar to the resonance effects previously discussed in connection with meteor trail echoes by Herlofson, Billam and Browne, Jones and Jones and others.

Keywords. Interplanetary physics (Interplanetary dust) – Radio science (Waves in plasma; Instruments and techniques)

1 Introduction

Meteor head echoes at UHF frequencies have now been systematically observed by high power, large aperture (HPLA) radar systems for more than 20 years. But even after this time, our understanding of the detailed characteristics of the plasma targets that create the head echoes is still inconclusive and there is not much substantive data on their actual size and shape. This is so primarily because the targets are much smaller than the spatial resolution of the radar systems and therefore remain unresolved. As an example, scattering cross sections observed by the EISCAT UHF system span a range of more than three decades (≈1 mm² to 40 cm²), thus putting an approximate upper limit to the effective plasma target diameter at 33 cm wavelength at about 7 cm – but the best range resolution that the radar can deliver is in the order of 100 m!

It has however been long recognised that the polarization of a radar echo will contain information about the shape and orientation of the radar target even when individual scatterers are much smaller than the radar wavelength. The meteorological community has been making operational use of this fact for decades to determine the type and amount of precipitation (raindrops, sleet, snowflakes...) detected by weather radar, and the literature abounds with publications on polarimetric S- and X-band weather radar systems and the results from these (e.g. Raghawan, 2003; Illingworth, 2003; Hogan et al., 2002).

Polarimetric weather radars operate at wavelengths that are 10...100 times greater than the sizes of the detected hydrometeors. Since the ratio between the wavelength of a typical HPLA system (30...70 cm) and a typical meteor head echo plasma target is also in this range, polarimetric head echo radar observations should yield information about the effective plasma target shape and orientation not accessible by any other means. But unfortunately, most HPLA radar systems available to the meteor community cannot determine
The only direct head echo polarization measurements at VHF and UHF published so far are those made with the ALTAIR 160-MHz and 422-MHz systems in 1998 (Close et al., 2000, 2002, 2011). Currently, the only other polarimetry-capable HPLA system in the world is the tristatic EISCAT UHF (Folkestad et al., 1983). Its two 32-m receive-only antennas at Kiruna, Sweden and Sodankylä, Finland are fitted with dual orthogonal linear (V/H) polarization feed systems that enable the antennas to be dynamically configured to match the polarization of the received incoherent-scatter signal. In a measurement series carried out in October 2009, we made use of this feature, together with the capability of the tristatic system to uniquely determine the vector velocities of head echo targets, to study the polarization of 930-MHz meteor head echoes for the first time.

2 The experiment

When the UHF radar is used in its “standard”, i.e. incoherent-scatter (IS), mode, the polarization of the incoherent-scatter signals received at the Kiruna and Sodankylä sites can take on any value from right-hand circular (RHC) via elliptical and linear to left-hand circular (LHC), depending on the location of the common scattering volume. In order to enable the Kiruna and Sodankylä 32-m antennas to recover as much as possible of the available echo power, their feed systems are fitted with waveguide orthomode transformers (OMTs) that split the intercepted signals into two orthogonal, linearly polarized components, oriented respectively along the local horizontal (H) and at right angles to the horizontal and the optical axis of the antenna (somewhat inappropriately labelled “V”). The V and H component signals are amplified in separate LNA systems. In the IS system configuration the amplified signals are then recombined into a single signal containing all the received power by a computer-controlled phase-shifting/summing passive four-port network (the “Polarizer”), which is set to make the polarization response of the antenna match that of the scatter signal.

Our observations employed the polarimetric capabilities latent in this front-end configuration for the first time in EISCAT history: the Polarizers were bypassed and the Kiruna and Sodankylä receiver systems reconfigured to process the H and V signals independently. After amplification and down-conversion to an intermediate frequency in the 10 MHz range in two separate but phase-coherent RF/IF chains, the H and V IF signals were sampled coherently by a dual-channel ADC and the two complex amplitude sample streams recorded to disk, so allowing subsequent sample-by-sample analysis. From these data, the V/H amplitude ratio and V-H phase difference of the received echo signal and, indirectly, the target polarization were determined.

The radar code used for our observations was a modified version of the “standard IRF meteor experiment” employed by the IRF radar meteor group since 2002 (Wannberg et al., 2008). The experiment geometry is shown in Fig. 1. A common scattering volume (in the following section referred to as $Q$), located at 96.0 km altitude vertically above (68.876° N, 21.880° E), is illuminated by left-handed circularly polarized (LHC) RF pulses transmitted from the UHF transmitter at Tromsø, Norway. In each 1656-μs radar cycle, a single low-sidelobe $32 \times 2.4 \mu s$ pseudo-random BPSK pulse sequence is transmitted at 929.6 MHz. Target returns are observed by all three receivers and the received signals are sampled, digitised and recorded at 0.6-μs time resolution, corresponding to a range resolution of 90 m.

3 Theory

In a bi-static radar measurement, the polarization vector of the EM wave intercepted by the receiving antenna, $P_{RX}$, can be expressed as:

$$P_{RX} = k \mathbf{G} (\theta, \phi, h, \text{ref}) \mathbf{S} \mathbf{T}$$

where $\mathbf{T}$ is a Jones vector (Jones, 1941) specifying the polarization of the transmitted wave ($|\mathbf{T}| = 1$) and $\mathbf{S}$ is a $2 \times 2$ matrix describing the polarization response of the scattering target. $\mathbf{G}$ is a $2 \times 2$ diagonal matrix representing the geometrical transformation from the transmitting site frame of reference to the receiving site frame of reference via a scattering point ($\theta, \phi, h, \text{"ref"}$), specified in terms of the azimuth and elevation angles towards it from a specified reference location “ref” and its height above ground $h$. $k$ is a normalisation factor selected to make $|P_{RX}| = 1$. The elements of $\mathbf{T}$ and $P_{RX}$ are the two orthogonal, linearly polarized components of the transmitted and received waves as measured in their respective local frames of reference.
The polarization of the signal transmitted by the Tromsø EISCAT UHF antenna can be freely selected by adjusting two high-power waveguide phase-shifters that are part of the antenna feed system. The system is normally set up to transmit a pure IEEE left-handed circularly polarized (LHC) signal, but if the phase-shifters are not accurately adjusted, the transmitted signal will also contain a small cross-polarized (RHC) component. Assuming that the transmitted signal is pure LHC, it can be expressed in Jones notation as a column vector whose upper element represents the H-component and the lower element the V-component of the transmitted signal:

\[
T_{LHC} = \frac{1}{\sqrt{2}} \begin{bmatrix} 1 \\ \exp(-i\frac{\phi}{2}) \end{bmatrix} = \frac{1}{\sqrt{2}} \begin{bmatrix} 1 \\ -i \end{bmatrix}.
\]  
(2)

We now consider the polarization of the scattered signal received at one of the receiver sites. For a path from Tromsø to Kiruna via our common observing volume at \(Q\),

\[
G_{TQK} = \begin{bmatrix} -0.5857 & -0.1720 \\ 0.5792 & 0.5947 \end{bmatrix}
\]

To establish a reference, we first consider a situation where the common volume contains only normal ionospheric E-region plasma. With a typical density of \(\approx 10^{10}\) m\(^{-3}\) the plasma electrons are uncorrelated and the scattered signal is incoherent.

Uncorrelated electrons scatter isotropically, so the polarization of the incident wave is conserved in the scattering process, i.e. \(S_B = 1\). The polarization of the scattered wave reaching the Kiruna antenna is thus entirely determined by the scattering geometry (Faraday rotation along the path from \(Q\) to the Kiruna receiver is estimated at \(<5^\circ\) and therefore neglected):

\[
P_K = \frac{1}{\sqrt{2}} G_{TQK} \cdot \begin{bmatrix} 1 \\ -i \end{bmatrix} = \frac{1}{\sqrt{2}} \begin{bmatrix} -0.5857 + 0.1720i \\ 0.5792 - 0.5947i \end{bmatrix}.
\]  
(3)

or in polar form (with the argument in degrees):

\[
P_K = \begin{bmatrix} 0.4316 \angle 163.6 \\ 0.5870 \angle -45.8 \end{bmatrix} = (0.4316 \angle 163.6) \begin{bmatrix} 1 \angle 0 \\ \rho \angle \phi \end{bmatrix}
\]  
(4)

where the V/H amplitude ratio \(\rho = 0.5870/0.4316 = 1.360\) and the relative (V-H) phase angle \(\phi = -45.8 - 163.6 = -209.4\) or 150.6 (mod 360).

The polarization of a received head echo signal \(P_{HE}\) can now be determined as

\[
P_{HE} = (0.4316 \angle 163.6) \begin{bmatrix} 1 \\ E_V(t)/E_H(t) \end{bmatrix}
\]  
(5)

where \(E_V\) and \(E_H\) are the complex-valued V and H signals and the averaging is over all radar returns recorded during the passage of a meteor target through the common volume. Head echoes received at Kiruna with \(\rho \approx 1.360\) and \(\phi \approx 150.6^\circ\) will represent almost isotropic targets. Conversely, significant deviations from the isotropic values in either parameter imply that the target has polarized the scattered wave. In this case, the target scattering matrix \(S_{target}\) can be determined by noting that \(S_{target}\) and \(P_K\) are related through

\[
S_{target} \begin{bmatrix} 1 \\ -i \end{bmatrix} = \sqrt{2} G_{TQK}^{-1} P_K
\]  
(6)

such that the elements of \(S_{target}\) can be found by fully expanding both members of Eq. (5) and identifying real and imaginary terms on the two sides of the equation. As will become apparent in the following, however, our experimental data turned out to be of such a nature that it could for the most part be understood in straightforward physical terms without going through a detailed analysis procedure.

For completeness, it should be pointed out that while the UHF antennas themselves exhibit exceptionally low crosstalk between the H and V polarizations (\(<-48\) dB), such that measurements made in the main lobe can safely be assumed to be unbiased by cross-polarization effects, the two receiver channels used to process the V and H signals have slightly different gains and group delays. Consequently, the apparent polarization of the processed signal, \(P_{K,app}\), is also slightly different from \(P_K\):

\[
P_K = C_K P_{K,app}
\]  
(7)

where \(C_K\) is the inverse of the Kiruna receiver system differential transfer function. In the present case, \(C_K\) was determined by an independent measurement two days before the actual observation and found to be very close to unity:

\[
C_K = \begin{bmatrix} 1 & 0 \\ 0 & 1.056 \end{bmatrix}
\]

This says that the gain of the H receiver channel is about 5.6 percent greater than the gain of the V channel, such that the V amplitudes must be corrected by an equal amount, but that the phase lengths of the two channels are practically identical, such that no phase angle correction is required. The amplitude correction is taken care of in the data-averaging step.

4 Observations and data

The data presented here were recorded during two nine-hour observing sessions, viz. 7 October 2009, 00:00:00–07:59:59 UTC and 8 October 2009, 00:00:00–07:59:59 UTC.

It was realised from the outset that the unfamiliar system configuration requirements would make our observations technically demanding and this did indeed prove to be the case. At an early stage in the analysis process, the data from the two Sodankylä receiver channels were found to be systematically linearly dependent. This fact, which was later established to be the result of a cabling mistake, made the Sodankylä data useless for polarization work, although still perfectly good for Doppler determination. All amplitude and
As follows: for each event, target range information and other parameters and their symbols are listed in Table 1 and the relationships between the target trajectory and the various probes are shown graphically in Fig. 2.

Figure 3 presents histograms of observed velocities (a), amplitude ratios (b) and V-H phase differences (c). The velocity distribution spans the range from 20 km s\(^{-1}\) to 68 km s\(^{-1}\). It does not show the clear bimodal characteristic seen in previous EISCAT UHF head echo observations (Kero et al., 2008a), but instead peaks broadly at about 40 km s\(^{-1}\), which is consistent with the distribution containing only morning-side data measured at a comparatively low altitude (96 km). The amplitude ratio \(\rho\) is very narrowly distributed, peaking at \(\rho = 1.53 \pm 0.14\); only three events exhibit an amplitude ratio deviating from the mean by more than 2 \(\sigma\).

The phase distribution of the full dataset is surprisingly broad and not very informative, but when the two observing sessions are handled separately, things become clearer. The 7 October phase distribution (26 events) is found to be well-behaved and narrow, peaking at \(\phi = (150.6 \pm 9.3)\) degrees. Two events deviate strongly from the mean, by respectively 1.8 \(\sigma\) and 2.0 \(\sigma\); these are in fact two of the three amplitude ratio outliers!

The 8 October data comprises 16 events, so the standard deviation of its phase distribution should a priori be expected to be about 27 % (3–5 degrees) larger than that of the data recorded on the previous day, everything else being equal. What is actually observed, however, is \(\phi = (197.2 \pm 29.5)\) degrees – over a 24-h period the mean phase appears to have

<table>
<thead>
<tr>
<th>Derived parameter</th>
<th>Symbol</th>
</tr>
</thead>
<tbody>
<tr>
<td>Angle between target trajectory and vertical</td>
<td>(\delta)</td>
</tr>
<tr>
<td>Angle between target trajectory and magnetic field</td>
<td>(\beta)</td>
</tr>
<tr>
<td>Angle between target trajectory and TQK mirror plane</td>
<td>(\gamma)</td>
</tr>
<tr>
<td>Peak signal power</td>
<td>(\text{pwr})</td>
</tr>
<tr>
<td>Target speed</td>
<td>(v)</td>
</tr>
<tr>
<td>Angle between target trajectory and horizontal feed probe</td>
<td>(H)</td>
</tr>
<tr>
<td>Angle between target trajectory and “vertical” feed probe</td>
<td>(V)</td>
</tr>
</tbody>
</table>

Doppler velocity components (\(v_{TQ}, v_{TQK}\) and \(v_{TQS}\)) are extracted from the data by the cross-correlation/matched-filter method described by Wannberg et al. (2008). The average echo amplitude ratio \(\rho = |E_V/E_H|\), the average phase angle \(\phi = \angle(E_V - E_H)\) and echo peak power are also extracted. To simplify the interpretation of the data, the velocity components are then transformed into a right-handed Cartesian system with its origin at the centre of the common scattering volume, \(Q\), and its axes oriented due south, due east and towards zenith. Following this transformation, the target speed \((v)\), the angle between the target trajectory and the vertical \((\delta)\), the angle between the target trajectory and the magnetic field \((\beta)\) and the angle between the trajectory and the TQK mirror plane \((\gamma)\) are computed. The derived parameters and their symbols are listed in Table 1 and the relationships between the target trajectory and \(\beta, \delta,\) and \(\gamma\) are shown graphically in Fig. 2.

Using the 4-\(\sigma\) detection criterion, about 900 head echoes were identified in the 18 h of monostatic (Tromsø) data. About 67 % of these were detected above and below the common scattering scattering volume (the Tromsø system was programmed to have about three times the range coverage of Kiruna and Sodankylä). Of the remaining 300 events, only 44 exceeded the 4-\(\sigma\) threshold also in the Kiruna and Sodankylä data. These tristatic events have been analysed as follows: for each event, target range information and

To avoid interpretation problems caused by noisy data, a very high detection threshold was employed. Only those echoes whose signal power rose above the receiver noise baseline by more than four times the baseline standard deviation were accepted as genuine. Our rationale for this was that clear signatures of polarization were expected to be seen only in the stronger echoes if any polarization existed in the first place. Weak echoes would either be associated with small targets, whose cross-sections would be well within the Rayleigh regime and which would therefore by definition scatter isotropically, or possibly be the result of scattering off extended volumes of enhanced but underdense plasma, in which case it is not clear if they should be classified as true head echoes. In either case, random noise would make the interpretation difficult. While it could be argued that this selection procedure introduces a systematic bias, it is also indisputable that it gives a correct representation of the polarization characteristics of the strong signal part of the head echo population to within the statistical accuracy of the available data.
shifted by some 46 degrees and the standard deviation increased to nearly three times the predicted value. A subsequent investigation of the Kiruna receiver system suggests that these large changes are most probably the result of instrumental drift and phase jitter suffered during the observing session, rather than indications of a physical process. Accordingly, we have chosen to exclude the 8 October phase data from the data analysis. However, since phase fluctuations of the magnitude observed do not affect the Doppler velocity determination or the average V/H amplitude ratio, these 8 October quantities are retained in the analysis.

5 Discussion

5.1 Short timescale behaviour

The availability of synchronously sampled pairs of amplitude data from both linear polarizations allows us to study the fine structure of individual head echo events. On a pulse-to-pulse (millisecond) time scale, most events are found to be well behaved in the sense that the signal amplitudes trace out a quasi-Gaussian that replicates the shape of the spatial overlap of the Tromsø and Kiruna antenna beams. We interpret this as indicating that the targets have remained compact during the whole traversal of the beam overlap volume.

In the data analysis process, the amplitude ratio $|E_V/E_H|$ and the phase angle $\angle(E_V-E_H)$ have been averaged over the entire extent of each event as described in the previous
Section. This procedure is justified and necessary because of an effect illustrated by Fig. 4a, which shows a typical, fairly strong event in which the variances of both the V and the H amplitude signals are more than twice as high as the noise baseline variance and therefore dominate the total variance. Inspecting the return from an individual radar pulse in full 0.6-µs time resolution (Fig. 4b and c) we see that even though both the V and the H signals are strong, the amplitude ratio varies randomly around a mean value of about 1.5 with at least one interval exceeding 1.9 and another dipping to about 1.35 for several consecutive samples each. This shows that the scattering process is essentially stochastic on a microsecond time scale, such that the concept of echo polarization is only meaningful in an average sense.

5.2 The main population – isotropic scattering

The only direct HPLA radar measurements of head echo polarization at UHF published so far are those made by the 422-MHz ALTAIR system (Close et al., 2000, 2002, 2011). In the first two of these papers, the authors found evidence only for isotropic scattering. In Close et al. (2011) a single, very strong and multi-peaked head echo exhibiting clear signs of polarization is described, but in the summary the authors point out that this is a singular case and that the majority of head echoes do not show these features. Also, in a previous EISCAT UHF study of the head echo RCS/meteor aspect angle relationship (Kero et al., 2008b), the scattering cross sections of individual meteors were found to be only very weakly dependent on the aspect angle. While this result

Fig. 4. Showing the passage of a typical head echo target through the common scattering volume at Q in 0.6-µs time resolution. Panel (a) shows the full event in raw amplitude format. The time interval between successive radar pulses is 1656 µs and the event lasts for 30 pulses or about 50 ms (the first four pulses are not shown). Panel (b) shows the development of the scattered signal during a single 76.8 µs radar pulse (pulse number 10, counting from the left). Panel (c) shows the V-H amplitude ratio during the same pulse.
was based only on total power measurements, it still implies that the scatterers must be close to isotropic and exhibit little or no polarization.

In order to test the isotropic scatterer hypothesis against our data, the relationships between the amplitude ratio $\rho$, the phase angle $\phi$ and the seven experimental observables listed in Table 1 have been investigated. Scatter plots of $\rho$ versus five of the observables are shown in Fig. 5a–e. All observables have also been correlated with $\rho$ and $\phi$. The correlations with $\rho$ have been computed both across the full 44-event dataset and also with the three “$+2\sigma$” events removed, while correlations with $\phi$ have only been computed for the 26-event 7 October data.

Fig. 5. Scatter plots of the relationships between the V/H amplitude ratio $\rho$ and five other derived target parameters, viz. (a) the angle $\beta$ between target trajectory and magnetic field, (b) the angle $\delta$ between target trajectory and vertical, (c) the angle $\gamma$ between target trajectory and the TQK mirror plane, (d) the target speed $v$ and (e) the peak signal power $P$. 
Table 2. Statistical correlations between $\rho$ and other observables. Student’s t-values and non-directional null hypothesis probabilities. All events included.

<table>
<thead>
<tr>
<th>Variable</th>
<th>Correlation coefficient</th>
<th>$t$</th>
<th>Non-directional null hypothesis probability</th>
</tr>
</thead>
<tbody>
<tr>
<td>$\delta$</td>
<td>0.387</td>
<td>2.687</td>
<td>0.010</td>
</tr>
<tr>
<td>$\beta$</td>
<td>0.329</td>
<td>2.231</td>
<td>0.031</td>
</tr>
<tr>
<td>$\gamma$</td>
<td>-0.091</td>
<td>-0.585</td>
<td>0.560</td>
</tr>
<tr>
<td>pwr</td>
<td>-0.294</td>
<td>-1.970</td>
<td>0.056</td>
</tr>
<tr>
<td>$v$</td>
<td>0.482</td>
<td>3.522</td>
<td>0.001</td>
</tr>
<tr>
<td>$V$</td>
<td>-0.103</td>
<td>-0.663</td>
<td>0.511</td>
</tr>
<tr>
<td>$H$</td>
<td>-0.218</td>
<td>-1.430</td>
<td>0.160</td>
</tr>
</tbody>
</table>

Fig. 6. Scatter plot showing the distribution of the points of origin of the observed events in azimuth-elevation space. 0$^\circ$ azimuth is due north, 90$^\circ$ is due east and 180$^\circ$ due south.

Normalized $\rho$ correlation coefficients, associated $t$-values and null hypothesis probabilities for the full dataset are listed in Table 2. The dependencies between $\rho$ and $\delta$, $\beta$, pwr and $v$ are all seen to be statistically significant at the 5 % level. On the other hand, $\rho$ is seen to be only weakly dependent on the orientation of the trajectory relative to the directions of the V and H probes in the Kiruna antenna feed and clearly statistically independent of $\gamma$.

Removing the three “$\pm 2 \sigma$” events from the dataset and repeating the exercise, the ($\rho - \beta$), ($\rho - \delta$) and ($\rho - v$) correlations all drop to very low values, such that all dependencies between $\rho$ and the target geometry are no longer statistically significant (Table 3). This demonstrates that the $\rho$ distribution of the 40-event head echo population contained in the ($\rho = 1.53 \pm 0.14$) interval is essentially independent of target-radar geometry and target speed.

Figure 6 shows how the directions of arrival of the observed targets are distributed in azimuth-elevation space. The distribution is fairly uniform over a solid angle slice from 50$^\circ$ to 160$^\circ$ azimuth, covering about one-third of the visible hemisphere. Referring to Fig. 5c, we find that the associated aspect angles at Kiruna range from -20$^\circ$ to 70$^\circ$ – but more than two-thirds of the echoes still display V/H amplitude ratios within $\pm 10 \%$ of the observed mean, $\rho_{\text{obs, mean}} = 1.53$. The observed amplitude ratio is clearly almost independent of the direction of arrival and aspect angle, in good agreement with the isotropic target hypothesis. It is slightly greater than the theoretically predicted V/H amplitude ratio for isotropic scattering in a TQK bistatic geometry, $\rho_{\text{iso}} = 1.36$, but the fact that the observed values are so narrowly clustered around $\rho_{\text{obs, mean}}$ with a standard deviation of only 0.14 suggests that the 1.2 $\sigma$ difference is an experimental bias, caused by the transmitted signal being slightly elliptically polarized rather than accurately circular. Recalling that the Tromso system can in fact transmit any arbitrary polarization, this is an entirely plausible hypothesis; in fact, it would only take an admixture of 0.4 $\%$ (-24 dB) RHC to explain the observed discrepancy!

The results from a correlation analysis of the 7 October phase dataset are summarised in Table 4. The dependencies between $\phi$ and $\delta$, $\gamma$ and pwr are all found to be statistically significant at the 5 % level and the correlations between $\phi$

Table 3. Same as Table 2 but with the three $>2\sigma$ outlier events removed from the dataset.

<table>
<thead>
<tr>
<th>Variable</th>
<th>Correlation coefficient</th>
<th>$t$</th>
<th>Non-directional null hypothesis probability</th>
</tr>
</thead>
<tbody>
<tr>
<td>$\delta$</td>
<td>0.084</td>
<td>0.520</td>
<td>0.60</td>
</tr>
<tr>
<td>$\beta$</td>
<td>0.068</td>
<td>0.420</td>
<td>0.68</td>
</tr>
<tr>
<td>$\gamma$</td>
<td>0.066</td>
<td>0.408</td>
<td>0.68</td>
</tr>
<tr>
<td>pwr</td>
<td>-0.441</td>
<td>-3.030</td>
<td>0.004</td>
</tr>
<tr>
<td>$v$</td>
<td>0.197</td>
<td>1.239</td>
<td>0.22</td>
</tr>
<tr>
<td>$V$</td>
<td>-0.042</td>
<td>-0.259</td>
<td>0.80</td>
</tr>
<tr>
<td>$H$</td>
<td>-0.162</td>
<td>-1.012</td>
<td>0.32</td>
</tr>
</tbody>
</table>

Table 4. Statistical correlations between $\phi$ and other observables. Student’s t-values and non-directional null hypothesis probabilities for the 7 October events.

<table>
<thead>
<tr>
<th>Variable</th>
<th>Correlation coefficient</th>
<th>$t$</th>
<th>Non-directional null hypothesis probability</th>
</tr>
</thead>
<tbody>
<tr>
<td>$\delta$</td>
<td>-0.301</td>
<td>-1.546</td>
<td>0.135</td>
</tr>
<tr>
<td>$\beta$</td>
<td>-0.239</td>
<td>-1.206</td>
<td>0.240</td>
</tr>
<tr>
<td>$\gamma$</td>
<td>-0.377</td>
<td>-1.994</td>
<td>0.058</td>
</tr>
<tr>
<td>pwr</td>
<td>0.701</td>
<td>4.815</td>
<td>0.000</td>
</tr>
<tr>
<td>$v$</td>
<td>-0.175</td>
<td>-0.871</td>
<td>0.392</td>
</tr>
<tr>
<td>$V$</td>
<td>0.452</td>
<td>2.482</td>
<td>0.020</td>
</tr>
<tr>
<td>$H$</td>
<td>0.439</td>
<td>2.394</td>
<td>0.024</td>
</tr>
</tbody>
</table>
and $\beta$ and $v$ are also fairly significant. Interestingly, all these correlations remain at about the same level of significance even after removing the two “$+2\sigma$” events from the dataset.

However, with a standard deviation of only 9.3 degrees (i.e. less than 3% of a full period) the phase distribution is very narrow indeed, which further strengthens the case for isotropy. Figure 7 shows how the 7 October events are distributed in $\rho - \phi$ space. Of the 26 resolved tristatic events, 19 are clustered within $(\rho_{\text{mean}} \pm \sigma_{\rho}, \phi_{\text{mean}} \pm \sigma_{\phi})$. Three events deviate by a little more in amplitude ratio (up to 1.5 $\sigma$) but at the same time they are within 0.5 $\sigma_{\phi}$ of the mean phase. Only three events are genuine outliers. Thus 90% of the target returns show essentially the same V/H amplitude ratio and the same $E_{\text{V}} - E_{\text{H}}$ phase difference, independent of direction of arrival and aspect angle.

The only explanation consistent with these results is that a majority of the observed head echo targets do indeed scatter isotropically and impart no target-specific polarization signature to the scattered signal regardless of aspect angle. For that to be the case, the effective size of the scatterers must be in the Rayleigh regime, i.e. much smaller than half the radar wavelength (0.16 m), in good agreement with earlier estimates of 930-MHz effective target cross sections (Kero et al., 2008a, b).

In this context, we note that the strongly significant correlations between signal power and $\rho$ and $\phi$ cannot very well be manifestations of a target-related process. For that to be the case, such a cross-section-dependent process would have to be spatially isotropic but at the same time also control the amplitudes and phases of the signals received on the V and H probes, which are fixed in the lab system. This is a self-contradiction. Instead, we interpret these correlations as signatures of a systematic experimental error, probably caused by differential non-linearity in the two analogue channels of the Kiruna receiver as the echo signal amplitudes approach the upper limit of the receiver dynamic range.

5.3 The outliers – polarized echoes

As explained in Sect. 3, radar returns with V/H amplitude ratios much greater or smaller than the isotropic scattering value are clear signatures of target polarization. Our dataset contains three such events, whose amplitude ratios deviate by more than plus or minus 2 $\sigma_{\rho}$ from the mean/isotropic value, viz. $\rho = 1.87$, $\rho = 1.96$ and $\rho = 1.16$.

Referring to Fig. 5b and c, we note that the trajectories of the two high-$\rho$ events are very close to the horizontal and the TQK bistatic mirror plane, while the trajectory of the low-$\rho$ event is very close to the vertical and the magnetic field. Since the H probe of the Kiruna antenna is approximately parallel to the horizontal through $Q$, these measured V/H amplitude ratios can be directly interpreted in terms of the ratio of the transverse and longitudinal cross sections. The high-$\rho$ events, whose trajectories are close to parallel to the H probe direction, show vertical amplitudes that exceed the isotropic value by 22 and 28%, while the low-$\rho$ event, which is almost orthogonal to the H probe, shows about 32% excess horizontal amplitude. These observations demonstrate that some head echo targets do in fact show signs of polarization, but the effects are relatively weak and only likely to be noticed when the targets are observed under close to optimal conditions to begin with, i.e. in a geometry approaching the classical normal incidence trail echo case or in the same plane as one of the receiver antenna probes.

In all three cases, the effective transverse-to-trajectory scattering cross section is 50–70% greater than the longitudinal-to-trajectory cross section. This is surprisingly similar to the classical transverse cross section enhancement effect first predicted by Herlofson (1951), experimentally verified in trail echo experiments in the 1950s (Clegg and Closs, 1951; Billam and Browne, 1956; Greenhow and Neufeld, 1956), revisited by numerical methods in 1968–1969 (Lebedinec and Sosnova, 1967) and more recently discussed in the context of oblique scattering by Jones and Jones (1991); the observed enhancement is in the right direction and the magnitude is of the right order.

The classical transverse cross section enhancement effect is caused by a charge-separation plasma resonance, which can be excited in bounded plasma. In the classical meteor trail case the required boundary conditions are fairly well met in the radial direction at early times, when the plasma has just expanded to the initial radius $r_0$. For underdense trails the effect maximises as the plasma dielectric on the trail axis goes through $\varepsilon_{\text{pl}} \approx -1.4$ (Kaiser and Closs, 1952). The resonance will be observable as long as the trail plasma is

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tion is often taken to be complete after about ten collisions or \((2\ldots8) \times 10^{-4} \text{s}\) at 95 km altitude and 40 km s\(^{-1}\) meteor speed. At this time the trail is already several tens of meters long, so the boundary conditions necessary for the resonance to be excited are not present in the lengthwise direction and no cross section enhancement will occur for a wave with E-field vector parallel to the trail. Accordingly, all the early attempts to observe the plasma resonance effect experimentally (Clegg and Closs, 1951; Billam and Browne, 1956; Greenhow and Neufeld, 1956) were made at wavelengths in the \((4\ldots6 \text{ m})\) range, such that \(\lambda_{\text{rad}}/2\pi \geq 0.64 \text{ m}\), and transverse cross section enhancement was indeed observed.

By contrast, the three polarized events discussed here have been recorded at a wavelength of 0.33 m, such that \(\lambda_{\text{rad}}/2\pi = 5.3 \times 10^{-2} \text{ m}\) or less than one-third of \(r_0\) at the interaction altitude. They are similar to the generic head echo in most aspects: they are instantaneous, their cross sections are in the order of at most a few times \(10^{-4} \text{ m}^2\) and no traces of a trail echo can be detected. This implies that the characteristic size of the effective plasma target is in the order of a few centimetres, in accordance with the cross section data previously reported by e.g. Kero et al. (2008b). However, the clear signatures of transverse polarization indicate that these targets do not scatter isotropically, the most likely explanation being that the plasma distribution immediately behind the meteoroid is non-spherical with a transverse extent small enough to sustain a \((\lambda_{\text{rad}} = 0.33 \text{ m})\) plasma resonance.

The currently best available data on the development of meteor plasma at very early times is probably Dyrud et al. (2007). A subpart of their Fig. 3, which presents results from a numerical simulation of plasma generated by a \(40 \text{ km s}^{-1}\) meteor producing \(10^{12} \text{ electrons m}^{-1}\), is reproduced by permission here as Fig. 8. We see that the plasma distribution in the immediate vicinity of the meteoroid is drop-shaped and elongated along the trajectory. Next to the meteoroid the \(f_{\text{pl}} = 4.0 \times 10^7 \text{ Hz}\) isodensity contour falls at a radial distance of about ten Debye lengths or 5.0\ldots10.0 cm, but in the tailward direction the same isocontour extends to more than thirty Debye lengths or 15\ldots30 cm behind the meteoroid (Debye lengths in the ionosphere near 100 km altitude are of the order of 0.5\ldots1 cm). Assuming a larger meteoroid producing several times \(10^{13} \text{ e}^{-} \text{ m}^{-1}\) and further assuming that the head plasma generated by this meteor would develop in approximately the same way as in Fig. 8, the plasma should be marginally able to sustain a charge separation resonance at 930 MHz in the transverse direction, but in the longitudinal direction the resonance would be more strongly damped, leading to a relative enhancement of the transverse cross section in qualitative agreement with our observations. Collisional damping would be insignificant for either polarization since the EISCAT UHF frequency is more than two orders of magnitude higher than the plasma-neutral collision frequency.

To the extent that the data in Fig. 8 is representative of the early time plasma development, all head echo plasma

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**Fig. 8.** Results from a simulation of early time meteor plasma, reproduced from Dyrud et al. (2007) by permission. The meteor simulated here was moving against the surrounding atmosphere at 40 km s\(^{-1}\), i.e. at about the average speed of our event population, and was producing \(10^{12} \text{ ions/meter}\). The axes are in units of local ion Debye length \(l_D\): in the ionosphere near 96 km altitude \(l_D\) is of the order of 0.5\ldots1 cm. The electron density \(n_e\) is represented in terms of equivalent plasma frequency: orange \(\leftrightarrow n_e \approx 5 \times 10^{13} \text{ m}^{-3}\), violet \(\leftrightarrow n_e \approx 6 \times 10^{14} \text{ m}^{-3}\) and black \(\leftrightarrow n_e \approx 7.5 \times 10^{15} \text{ m}^{-3}\). Part (a) shows the plasma density distribution out to 400\(l_D\) behind the meteoroid, while panel (b) is a magnification of the region in the immediate vicinity of the meteoroid; the full contour line corresponds to \(n_e \approx 2 \times 10^{14} \text{ m}^{-3}\).

\(r_0\) is defined as the rms transverse separation of the meteor atoms from the parent meteor trajectory at the point where they have reached thermal equilibrium with the neutrals. Estimates of \(r_0\) range from three neutral free paths or about 16 cm at 96 km altitude (Manning, 1958) to more than one metre (Öpik, 1958; Bronshten, 1983). Thermalisation is radially confined to \(r_0 < \lambda_{\text{rad}}/2\pi\), but as the plasma expands to larger radii it will be progressively suppressed by radiative damping.
targets are actually anisotropic to some degree. Since the above analysis demonstrates that transverse charge separation plasma resonance in the plasma cloud moving with the ablating meteoroid is possible, this could give reason for concern when attempting to derive meteor size and mass from observed head echo cross sections. But our observations indicate that, at least at 930 MHz, resonant cross section enhancement only seems to be observable when the meteor trajectory is either within some 15° from normal to the scattering vector, i.e. close to Bragg conditions, or close to the vertical. Most events will therefore be unaffected and appear as isotropic targets, in excellent agreement with the conclusions from previous head echo aspect sensitivity studies (Dyrud et al., 2007; Kero et al., 2008b).

It is also interesting to note that close-in polarization effects may only be readily detectable at frequencies in the (800–1600) MHz range. If the Fig. 8 plasma were illuminated at 442 MHz (ALTAIR), longitudinal damping would only just begin to set in, such that some resonant longitudinal cross section enhancement would also be present – but this would reduce ρ and make the target look closer to isotropic. Conversely, at wavelengths much less than 20 cm even the transverse charge separation resonance would be damped out.

6 Summary and conclusions

This paper presents the first-ever direct measurements of the polarization of 930-MHz radar meteor head echoes, performed with the tristatic EISCAT UHF radar system in an oblique scattering geometry. Amplitudes and phases of two orthogonal, linearly polarized components (V and H) of head echo signals recorded with the Kiruna UHF receiver have been used to determine the V/H amplitude ratio and (V-H) phase difference and both quantities have then been correlated with the target aspect angle, 3-D target velocities and a range of other parameters.

While the 44 analysed events are relatively uniformly spread over one-third of the visible hemisphere, more than 90% of them still show essentially the same amplitude ratio and phase difference that would have been observed if the radar target had instead been an incoherent plasma. No significant correlation is found to exist between the observed amplitude ratio and phase difference and target aspect angle, direction of arrival and echo strength.

Only three events, two of which are observed under close to Bragg conditions and the third coming in on an almost vertical trajectory, show clear signatures of polarization. In all three cases, the effective transverse-to-trajectory scattering cross section is 50–70% greater than the longitudinal cross section. We propose that this could be a signature of a transverse charge-separation resonance in the plasma immediately behind the meteoroid, similar to the classical trail echo transverse cross section enhancement first discussed and observed in the 1950s. We show that the densest part of the ablated plasma column is small enough to support a transverse plasma resonance at the EISCAT UHF frequency, 930 MHz and note that the effect may only be readily observable over a relatively narrow range of wavelengths that includes the EISCAT UHF but not ALTAIR and other low-UHF systems.

We conclude that a majority of the tristatic high-SNR head echoes observed by us appear isotropic in backscatter. This suggests that, at least at 930 MHz, strong and compact (i.e. non-fragmenting) head echo events can in general be safely assumed to represent isotropic scatterers, in good agreement with previous polarization work at 422 MHz and EISCAT UHF cross-section vs. aspect angle studies. We postulate that this also holds true for compact low-SNR targets, such that polarization effects should not play a significant role when deriving meteoroid sizes and masses from the observed head echo radar cross sections.

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