Low-frequency magnetic field fluctuations in Venus’ solar wind interaction region: Venus Express observations

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Abstract. We investigate wave properties of low-frequency magnetic field fluctuations in Venus’ solar wind interaction region based on the measurements made on board the Venus Express spacecraft. The orbit geometry is very suitable to investigate the fluctuations in Venus’ low-altitude magnetosheath and mid-magnetotail and provides an opportunity for a comparative study of low-frequency waves at Venus and Mars. The spatial distributions of the wave properties, in particular in the dayside and nightside magnetosheath as well as in the tail and mantle region, are similar to observations at Mars. As both planets do not have a global magnetic field, the interaction process of the solar wind with both planets is similar and leads to similar instabilities and wave structures. We focus on the spatial distribution of the wave intensity of the fluctuating magnetic field and detect an enhancement of the intensity in the dayside magnetosheath and a strong decrease towards the terminator. For a detailed investigation of the intensity distribution we adopt an analytical streamline model to describe the plasma flow around Venus. The orbit geometry is very suitable to investigate the fluctuations in Venus’ low-altitude magnetosheath and mid-magnetotail and provides an opportunity for a comparative study of low-frequency waves at Venus and Mars. The spatial distributions of the wave properties, in particular in the dayside and nightside magnetosheath as well as in the tail and mantle region, are similar to observations at Mars. As both planets do not have a global magnetic field, the interaction process of the solar wind with both planets is similar and leads to similar instabilities and wave structures. We focus on the spatial distribution of the wave intensity of the fluctuating magnetic field and detect an enhancement of the intensity in the dayside magnetosheath and a strong decrease towards the terminator. For a detailed investigation of the intensity distribution we adopt an analytical streamline model to describe the plasma flow around Venus. This allows displaying the evolution of the intensity along different streamlines. It is assumed that the waves are generated in the vicinity of the bow shock and are convected downstream with the turbulent magnetosheath flow. However, neither the different Mach numbers upstream and downstream of the bow shock, nor the variation of the cross-sectional area and the flow velocity along the streamlines play probably an important role in order to explain the observed concentration of wave intensity in the dayside magnetosheath and the decay towards the nightside magnetosheath. But, the concept of freely evolving or decaying turbulence is in good qualitative agreement with the observations, as we observe a power law decay of the intensity along the streamlines. The observations support the assumption of wave convection through the magnetosheath, but reveal at the same time that wave sources may not only exist at the bow shock, but also in the magnetosheath.

Keywords. Magnetospheric physics (MHD waves and instabilities; Solar wind interactions with unmagnetized bodies) – Space plasma physics (Turbulence)

1 Introduction

Waves in plasmas, which are generally considered as fluctuations in the electric field, the magnetic field, the density, and the temperature, play an important role in the interaction processes of the solar wind with planets and other solar system bodies. Because the particle densities in space plasmas surrounding the obstacles are low, collisions between particles occur rarely and the transfer of momentum and energy can only be accomplished by waves. Hence, it is important to study wave characteristics, their origins, and generation mechanisms in order to improve our understanding of the complex interaction processes. Many observations of waves in the ultra-low-frequency and low-frequency range at various planets are reported (e.g. Glassmeier and Espley, 2006). Above all, it is interesting to study the plasma environment.
of Venus, because it does not possess an intrinsic magnetic field and the solar wind interaction is similar to that at Mars (e.g. Cloutier et al., 1999), also lacking a global planetary magnetic field (e.g. Acuña et al., 1998). A statistical study of low-frequency magnetic field oscillations in the Martian plasma environment is presented by Espley et al. (2004).

Since the early 1960s Venus has been an object of exploration by more than 20 spacecraft missions from the United States and the former Soviet Union. However, most of the current understanding of the solar wind interaction with Venus comes from the Pioneer Venus Orbiter (PVO) due to its long-lasting mission from 1978 to 1992 (Russell, 1991). At Venus the solar wind interacts directly with the planet’s upper atmosphere, creating various boundaries and regions in the Venusian plasma environment (e.g. Luhmann, 1986). Observations of plasma waves, mainly detected by the Orbiter Electric Field Detector (OEFD) on board the PVO at frequencies from 100 Hz to 30 kHz are summarised by Huba and Strangeway (1997) and Strangeway (1991) and are compared to observations at Mars by Strangeway (2004). The temporal resolution of the PVO magnetometer samples reaches 12 Hz (Russell et al., 1980) and thus allows to investigate magnetic field fluctuations up to a few Hz. Waves upstream of the Venusian bow shock have been studied by Orlowski et al. (1994) and Strangeway and Crawford (1995). Downstream of the bow shock Brace et al. (1983) detected ionospheric wave structures nightward of the terminator which they call post-terminator ionospheric waves. Large magnetic field fluctuations in the magnetosheath of Venus with periods from 10 to 40 s have been observed by Luhmann et al. (1983). They supposed that these waves are generated most likely in the vicinity of the quasi-parallel bow shock and are convected downstream in the magnetosheath with the solar wind plasma. Their possible origin has been studied by means of numerical simulations by Winske (1986), suggesting that plasma instabilities can generate these waves either directly by the interaction of the solar wind with the quasi-parallel bow shock or with the oxygen ions of planetary origin (pickup ions). Luhmann (1995) investigated magnetic field fluctuations in the low-altitude subsolar magnetosheath and found predominantly linearly polarised waves of transverse character with regard to the background magnetic field which have also been observed at Earth. Grebowsky et al. (2004) observed ultra-low-frequency waves in the vicinity of detected ion pickup regions which suggest an association of wave generation with the pickup ions.

The current knowledge about Venus and its space environment is now further completed by the Venus Express spacecraft, the first European mission to the planet Venus (Titov et al., 2006). Launched in November 2005, the spacecraft arrived at Venus in April 2006 and was inserted into a polar orbit with a period of 24 h. The orbit geometry of Venus Express allows magnetic field measurements in the low-altitude region near the terminator and the mid-magnetotail region which were not covered by the PVO (Zhang et al., 2006). The better coverage of the Venusian dayside and nightside magnetosheath as well as the magnetotail provides an opportunity to study statistically magnetic field fluctuations in these regions in more detail. Recently, proton cyclotron waves upstream of the Venusian bow shock (Delva et al., 2008a,b,c) and mirror mode structures in the magnetosheath (Vörös et al., 2008a,b) have been detected using the magnetic field measurements of the fluxgate magnetometer on board the Venus Express spacecraft (Zhang et al., 2006). Vörös et al. (2008a,b) studied properties of magnetic field fluctuations in the Venusian magnetosheath and wake and observed varying scaling features of the fluctuations in the different regions.

In this work we present a statistical study of magnetic field fluctuations near Venus in the low-frequency regime. We adopt the definition given by Espley et al. (2004) who refer frequencies near or below the proton gyrofrequency as the low-frequency range and frequencies below the lowest local ion gyrofrequency as the ultra-low-frequency range. As Espley et al. (2004) provide a statistical study of low-frequency magnetic field oscillations at Mars, including the magnetosheath, the magnetic pileup region, and the tail, our study provides also the basis for a comparative wave study between Venus and Mars.

2 Data and analysis methods

In this study we use a Venus Express magnetometer data set which includes 567 orbits between April 2006 and December 2007 with a temporal resolution of 1 s. The data are corrected for perturbations caused by the spacecraft so that the data have an accuracy of about 1 nT for the absolute field and an accuracy better than 0.1 nT for the variable field. This accuracy has been realised by a novel software procedure applied to the dual-sensor measurements of the Venus Express magnetometer (Zhang et al., 2008a,c). The data set is given in the Venus solar orbital (VSO) coordinate system in which the x-axis points towards the sun, the y-axis is in the opposite direction to the planetary orbital motion and the z-axis completes the right-handed coordinate system pointing northward from the orbital plane. In order to take into account the orbital velocity of Venus with respect to the mean solar wind velocity, we adopt the aberrated VSO coordinate system (x′,y′,z′) suggested by Martinecz et al. (2008) for the presentation of the results. The transformation to the aberrated VSO coordinate system (VSO′ coordinate system) is realised by a constant rotation of 5° around the z-axis.

Figure 1 shows the spatial distribution of the observed magnetic field strength in a cylindrical coordinate system in which the magnetic field strength is averaged over the directions around the x′-axis. So, the cylindrical symmetry is assumed with regard to the x′-axis, leading to a two-dimensional picture with the axes x′cyl = x′ and y′cyl = \sqrt{y'^2 + z'^2}. This means that the x′cyl-axis represents the apparent solar wind direction and the y′cyl-axis the distance...
Fig. 1. Spatial distribution of the magnetic field strength in the plasma environment surrounding Venus. The measurements are averaged around the axis of the apparent solar wind direction ($x'_{cyl}$). Downstream of the bow shock (BS) the magnetic field strength is enhanced relative to the solar wind region upstream of the bow shock and piles up towards the terminator in the low-altitude dayside magnetosheath forming the magnetic barrier. Draping of the magnetic field around the planet leads to the formation of the magnetotail which is characterised by a slightly enhanced magnetic field strength in the planet’s wake, too.

For our statistical study intervals with the time length 100 s are selected with a shift of 1 s from one interval to another. Gaps in the data set greater than 1.5 s are excluded from the analysis. The interval length is chosen as a trade-off between the temporal and spatial resolution as well as the occurrence of data gaps. With respect to the bin size that means that almost every bin is well covered by observations which is shown in Fig. 2. The statistical analysis is performed in the frequency range 30 to 300 mHz, as we focus on low-frequency magnetic field fluctuations. The lower boundary of this frequency range acts as a band-pass filter such that oscillations with periods longer than 33 s do not contribute to the statistical results. The gyrofrequency is defined as $\omega = qB/m$ where $B$ is the magnetic field strength and $q$ and $m$ are the electric charge and the mass of the ion species. The upper boundary of the analysed frequency range, 300 mHz, corresponds to the proton gyrofrequency at a field strength of about 20 nT, a typical magnetic field strength in the Venustian magnetosheath (Fig. 1); therefore the frequency range well covers the low-frequency range in Venus’ solar wind interaction region. In spite of that, we realise that it is also attractive to expand or reduce the frequency band depending on the conditions in specific regions (e.g. with respect to the gyrofrequency) which would allow a comparison of...
different frequency bands. In particular, studying the ultra-
low-frequency range in more detail would be worthwhile, but
we mention again that increasing the frequency resolution is
at the expense of the spatial resolution and is thus always a
balancing issue.

Spectral analysis is widely used in order to determine wave
properties such as the wave power, ellipticity, polarisation,
and propagation direction. The wave analysis methods are
well developed by e.g. Arthur et al. (1976); Samson (1973);
McPherron et al. (1972); Means (1972); Sonnerup and Cahill
(1967) and are frequently applied to space time series data.
The methods are based on several assumptions and there are
also limitations. First of all, the analysis method is based on
the assumption of plane waves and there is an ambiguity of
±180° in determining the propagation direction of the waves
as one determines the minimum variance direction only. This
comes from the fact that the magnetic field is measured by a
single spacecraft. Furthermore, from single spacecraft mea-
surements one can only determine wave parameters in the
spacecraft frame of reference which is subject to the Doppler
shift of frequencies, when the measurements are made in a
flow. The analysis of a certain frequency band, finally, leads
to averaged wave parameters for this frequency band.

The wave analysis is performed as follows: (1) The mag-
netic field components of each time interval are transformed
to a mean field aligned (MFA) coordinate system in which
the principal direction (z-axis) is defined as the direction of
the mean magnetic field in the interval, the second direction
(x-axis) is perpendicular to the plane spanned by the vector
pointing into the new z-direction and the spacecraft position
vector in VSO coordinates, and the third direction (y-axis)
completes the right-handed coordinate system. This transfor-
mation allows us to distinguish between the transverse and
the compressional power of the fluctuations with respect to
the mean magnetic field. (2) The data in the MFA system are
Fourier transformed into frequencies. (3) With the Fourier
transform $B(w)$ we calculate the power spectral density ma-
trix $P$ for the selected frequency range

$$P_{ij} = \langle B_i(w)B_j^*(w) \rangle,$$

where $i$ and $j$ are the three components of the magnetic
field ($i, j = 1, 2, 3$) and the asterisk denotes the complex-
conjugate. The power spectral density matrix is a $3 \times 3$ com-
plex matrix and can therefore be written as the sum of its real
and imaginary part ($P_{ij} = \text{Re}(P_{ij}) + i\text{Im}(P_{ij})$). In the MFA
system two diagonal elements, $P_{11}$ and $P_{22}$, represent an
estimate of the transverse power, whereas $P_{33}$ corresponds to
the compressional power. (4) Finally, the principal axis anal-
ysis is applied in order to determine the minimum and max-
imum variance directions. In particular, diagonalisation of
the real part of the power spectral matrix yields three eigen-
ectors ($\xi_1, \xi_2, \xi_3$) and three eigenvalues ($\lambda_1, \lambda_2, \lambda_3$) for the
maximum, intermediate, and minimum variance directions,
respectively. The matrix of the three eigenvectors $T$ can then

![Observational coverage](image_url)

**Fig. 2.** Observational coverage. Almost every bin is well covered by observations, but the spatial distribution is not homogenous. The polar orbit of Venus Express provides in the vicinity of the pericentre relatively more observations.
Fig. 3. Example of the analysis in the interval from 01:27:54 UTC to 01:29:34 UTC on 25 May 2006: (a) displays the three components of the magnetic field in VSO and MFA coordinates as well as the magnetic field strength. The mean magnetic field strength is 38 nT corresponding to the proton gyrofrequency \( f_{\text{gyro}} = 580 \text{ mHz} \); (b) shows a sketch of the orbit in the dayside plasma environment close to Venus in cylindrical VSO\(^{\prime}\) coordinates. The black rectangle denotes the analysed time interval; (c) shows the power spectra of the magnetic field data in the frequency range from 30 to 500 mHz of the total power (\( P_{\text{total}} \)) as well as the transverse (\( P_{\perp} \)) and the compressional (\( P_{\parallel} \)) component (here a window function is applied to the spectra in order to increase the significance of the structures, but the spectra do not exhibit spectral peaks larger than the 95% confidence interval in this single spectrum). The dotted straight line indicates a linear fit in the logarithmic scaled spectrum revealing the spectral index \( \alpha = -1.56 \).

be used to transform the entire spectral matrix \( \mathbf{P} \) into the principal axis (PA) system via \( \mathbf{P}' = \mathbf{T}^{-1} \mathbf{P} \mathbf{T} \). Various wave properties are derived from the spectral matrix, the eigenvectors, and the eigenvalues and the results are presented in the following section. Here one should note that the propagation direction of the wave is well determined only if the intermediate eigenvalue is sufficiently larger than the minimum eigenvalue, otherwise the fluctuations are isotropic and the polarisation plane is not clearly determined.

3 Results

The analysis procedure in the previous section is demonstrated for one interval (25 May 2006, 01:27:54 UTC–01:29:34 UTC). In this time interval Venus Express is located in the high-latitude dayside magnetosheath. Figure 3 shows the magnetic field components in VSO (first to third panel in Fig. 3a) and MFA coordinates (fourth to sixth panel in Fig. 3a) as well as the magnetic field strength (bottom panel in Fig. 3a), the orbit trajectory in the cylindrical VSO\(^{\prime}\) co-ordinate system (Fig. 3b) and the power spectrum (Fig. 3c). The mean magnetic field is 38 nT corresponding to the proton gyrofrequency \( f_{\text{gyro}} = 580 \text{ mHz} \).

The field components in the MFA coordinate system are Fourier transformed and the transverse Power \( P_{\perp} \) and the compressional power \( P_{\parallel} \) are determined from the power spectral density matrix.
We furthermore define the quantity $\zeta$ as

$$\zeta = \frac{P_\perp - P_\parallel}{P_{\text{total}}}(2)$$

which is positive in the case of dominating transverse power and negative in the case of dominating compressional power. In the example interval we obtain the value $\zeta = 0.31$, therefore the transverse power exceeds the compressional one. This can also be seen in the power spectrum plot (Fig. 3c) in which the dashed line represents the transverse power spectral density $P_\perp$ and the dashed-dotted line the compressional power $P_\parallel$. After rotation into the PA coordinate system, we obtain further parameters describing the wave properties, namely the ellipticity, the sense of polarisation, the propagation directions, and the intensity. The absolute value of the ellipticity $|\epsilon|$ can be determined from the eigenvalues and is defined as (Song and Russell, 1999)

$$|\epsilon| = \sqrt{\frac{\lambda_2 - \lambda_3}{\lambda_1 - \lambda_3}}(3)$$

assuming isotropic noise which means that $\lambda_3$ corresponds to the noise in the $k$-direction. The sign of $\epsilon$ is the same as the sign of $\text{Im}(P_{12}')$. The average sense of polarisation over the frequency band yields the value $\epsilon = -0.72$ which indicates a slightly increased left-handed polarisation for the selected frequency band. Furthermore, the angle between the minimum variance direction and the mean magnetic field is about $90^\circ$, so the wave vector direction is practically perpendicular to the mean magnetic field. Finally, the intensity of the fluctuations $I$ is defined as (Song and Russell, 1999)

$$I = \lambda_1 + \lambda_2 - 2\lambda_3. (4)$$

The intensity is a mean spectral density of the chosen frequency band and we obtain $I = 157.2\ \text{nT}^2/\text{Hz}$. The intensity is an estimate of the total magnetic energy density in the frequency range 30 to 300 mHz. In summary, the analysis of the wave properties in this example exhibits dominating transverse, slightly left-handed polarised fluctuations with a large propagation angle relative to the mean field and enhanced wave intensity. We apply this analysis procedure to all available time intervals of the data set. The spatial distributions of various wave parameters are presented in the same fashion as in Fig. 1.

**Fig. 4.** Difference between the transverse and compressional power normalised to the total power about the mean field. The coordinate system is the same as in Fig. 1. Blue regions indicate regions where the transverse power dominates ($\zeta = +1$ purely transverse) and red regions where the compressional power dominates ($\zeta = -1$ purely compressional). In the vicinity of the dayside bow shock the magnitude of transverse and compressional power are of the same size, whereas in the vicinity of the nightside bow shock the compressional portion increases. In the dayside magnetosheath as well as in the mantle and tail region the compressional power is slightly higher than the compressional power in the nightside magnetosheath. In the solar wind upstream of the bow shock the transverse portion of the power dominates over the compressional portion.
Ellipticity

Fig. 5. Ellipticity of the waves in the space plasma environment surrounding Venus. The value $\epsilon = 0$ denotes a pure linear polarisation and $\epsilon = 1$ a pure circular polarisation.

3.1 Transverse vs. compressional power

Figure 4 displays the spatial distribution of the parameter $\zeta$, the difference between the transverse and compressional power relative to the total power. Some features can be observed here: in the vicinity of the dayside bow shock the transverse and compressional power are almost equal, whereas the compressional power tends to be slightly greater in the vicinity of the nightside bow shock, because of the increased occurrence of red-coloured bins. However, by no means the compressional power clearly dominates this region. In the dayside magnetosheath as well as in the mantle and tail region the compressional power is slightly higher than that in the nightside magnetosheath. But the transverse power still exceeds the compressional power. In the solar wind (upstream of the bow shock) the transverse power dominates over the compressional one.

3.2 Ellipticity

The spatial distribution of the ellipticity is presented in Fig. 5. On average the absolute value of the ellipticity $|\epsilon|$ reaches higher values in the magnetosheath (around 0.6) with respect to the upstream solar wind and the tail and mantle region. Though, the waves are only moderately polarised, rarely exceeding the value 0.6, but also a few regions exist where the ellipticity is less than 0.6. In the upstream solar wind and in the mantle and tail region the ellipticity values are rather mixed and no clear tendency can be observed.

3.3 Polarisation

Figure 6 shows the spatial distribution of the average sense of polarisation of the low-frequency magnetic field fluctuations. The distribution does not show any clear distinct regions of either dominating left-handed or right-handed polarisation close to Venus. At larger distances from the planet there are areas of enhanced polarisation. However, neither the magnetosheath nor the tail and mantle region show large-scale connected areas with a preferred sense of polarisation. It should also be noted that for almost linear polarisation it is not meaningful to discuss the sense of polarisation due to the error in the determination of the ellipticity; the results should be treated with care. Furthermore, direct comparisons to polarisations derived from theoretical studies can lead to misinterpretations, as the Doppler shift from the plasma frame to the spacecraft frame of reference may reverse the senses of polarisation. Waves which propagate downstream from the bow shock do not change the polarisation. This is only the case if the waves propagate in opposite direction to the solar wind flow with a phase velocity lower than the solar wind flow velocity (e.g. Hoppe and Russell, 1983). In this context one should note that on the one hand averaging over the absolute values of the ellipticity may shift the average of a bin away from zero, but on the other hand a reversal


3.4 Wave vector direction

As already mentioned in Sect. 2, the determination of the propagation direction or the wave vector direction is valid only, when the ratio of the intermediate to the minimum eigenvalue ($\lambda_2/\lambda_3$) is large enough. Espley et al. (2004) used a ratio of 2 as a criterion in order to determine the wave vector direction of low-frequency magnetic field oscillations in the Martian plasma environment. We note that according to Song and Russell (1999) high ratios are favoured, because the propagation direction is better determined for higher ratios of the eigenvalues. Therefore, we use a more stringent condition than Espley et al. (2004) and consider only cases with the intermediate to minimum eigenvalue ratio greater than 5. This is a compromise, because otherwise we lose a significant portion of the data set in the analysis. We accept possible limitations so far as we give a statistical result. Figure 7 shows the spatial distribution of the angle between the wave vector and the mean magnetic field in Venus' solar wind interaction region in the cases satisfying the specified eigenvalue ratio criterion. In Fig. 7 one can see that in the low-altitude dayside magnetosheath the wave vector directions are almost perpendicular to the mean magnetic field. Also in the mantle and tail region a majority of the angles reaches values greater than 45°, whereas in the nightside magnetosheath a tendency to smaller angles can be observed, in particular, events with an angle below 45° occur quite frequently. Data gaps in the magnetosheath are due to the selection criterion of the intermediate to minimum eigenvalue ratio. In the upstream solar wind the results are fairly mixed with a slight predominance of angles greater than 45°.

3.5 Intensity

The spatial distribution of the wave intensity $I$ about the mean field in the plasma environment surrounding Venus is presented in Fig. 8. The intensity is largest in the entire dayside magnetosheath and decreases rapidly towards the terminator region. In the nightside magnetosheath the intensity is still moderately enhanced in the vicinity of the bow shock, but further downstream and in the mantle and tail region only very small wave intensities can be observed. We would like to note that the lower end of the colour bar displaying the intensity in Fig. 8 is two orders of magnitude

![Fig. 6. Average sense of polarisation of the low-frequency magnetic field fluctuations in Venus’ space plasma environment. Blue colours indicate regions of dominating right-handed polarisation and red colours regions of dominating left-handed polarisation. Close to the planet a tendency to less distinct regions of either preferentially left-handed or right-handed polarised waves is observable. The other regions are locally dominated by right-handed or left-handed polarisation, but no connected areas of larger size with a preferential sense of polarisation is visible.](image_url)
above the threshold of the data accuracy. Almost all intensities are above this threshold and therefore the artificial contribution to our results is expected to be very small. In regions with lower intensities the wave property results may be subject of a somewhat increased uncertainty compared to regions with larger intensities, though. The wave intensity distribution is further investigated and discussed in more detail in the next section, as it may give a hint about how rapidly turbulence evolves in the magnetosheath. This is of great interest in fundamental plasma physics.

### 3.6 Spectral indices

Power spectra for the both transverse and compressional fluctuations exhibit a power law spectrum in the analysed frequency range. From our statistical analysis we have determined the average spectral indices of the total, transverse, and compressional power in the magnetosheath, mantle, and tail region (Table 1) providing an estimate of the different turbulent states. The spectral indices of the total power in the dayside and nightside magnetosheath are slightly flatter than in the mantle and tail region. Furthermore, in the dayside and nightside magnetosheath as well as in the mantle the spectral indices of the compressional component are steeper than the transverse ones. In the tail the decay of the transverse component is steepest.

### 4 Discussion

The statistical analysis reveals the wave properties of the low-frequency magnetic field fluctuations in various Venusian solar wind interaction regions. The observations are summarised and compared to the wave properties observed at Mars. We also investigate the spatial distribution of the intensity in more detail and discuss possible mechanisms and processes which may lead to the made observations.

#### 4.1 Wave properties at Venus and Mars

In the dayside magnetosheath and the vicinity of the bow shock the compressional and transverse power are approximately equal and the waves are moderately elliptically polarised with changing senses of polarisation. With larger distances from the planet the respective polarisation increases. Closer to the planet the senses of polarisation are not much pronounced. The wave vector has largest angles with respect to the mean magnetic field in the low-altitude magnetosheath and smaller angles at higher altitudes. The wave
intensity is enhanced in the entire dayside magnetosheath and drops rapidly at the terminator. Towards the nightside magnetosheath the transverse power increases and exceeds the compressional power in the majority of cases except for the regions close to the vicinity of the bow shock. The ellipticity is still moderate, but also in a few areas the ellipticity becomes lower and left-handed or right-handed senses of polarisation can locally be observed. A significant part of the angles between the propagation direction and the mean magnetic field has values below 45°, but they increase near the bow shock and the UMB. The wave intensity is significantly lower compared to the dayside magnetosheath, but in the vicinity of the bow shock areas of higher intensity are still present. The transverse and compressional power in the mantle and tail region are fairly mixed with a slight majority of areas in which the transverse power dominates. The ellipticity varies over a wider range compared to the magnetosheath and areas of locally dominated left-handed or right-handed polarisation also occur, but rather at larger distances from the planet. The wave vector directions have in most cases angles greater than 45° with respect to the mean magnetic field. The intensity is in the entire mantle and tail region at a very low level. In contrast, the upstream solar wind region is characterised by dominating transverse power with a broad spectrum of ellipticity values and various angles between the propagation direction of the waves and the mean field with no clear areas of enhanced wave intensity. The spectral indices (Table 1) indicate a turbulent behaviour of the magnetic field fluctuations at Venus. In particular, the magnetosheath reveals slightly smaller indices than expected.

Fig. 8. Spatial distribution of the wave intensity. The intensity is enhanced in the entire dayside magnetosheath and drops rapidly towards the terminator. In the nightside magnetosheath the intensity has a reduced level. No significant intensity occurs in the upstream solar wind and the mantle and tail region.

Table 1. Observed spectral indices with its standard deviations of the mean in Venus' solar wind interaction region. The values in brackets represent the sample standard deviations.

<table>
<thead>
<tr>
<th>region</th>
<th>component</th>
<th>spectral index</th>
</tr>
</thead>
<tbody>
<tr>
<td>dayside magnetosheath</td>
<td>total</td>
<td>$-1.854 \pm 0.001 \ (0.588)$</td>
</tr>
<tr>
<td></td>
<td>transverse</td>
<td>$-1.783 \pm 0.001 \ (0.622)$</td>
</tr>
<tr>
<td></td>
<td>compressional</td>
<td>$-1.988 \pm 0.001 \ (0.660)$</td>
</tr>
<tr>
<td>nightside magnetosheath</td>
<td>total</td>
<td>$-1.879 \pm 0.001 \ (0.639)$</td>
</tr>
<tr>
<td></td>
<td>transverse</td>
<td>$-1.851 \pm 0.001 \ (0.696)$</td>
</tr>
<tr>
<td></td>
<td>compressional</td>
<td>$-1.950 \pm 0.001 \ (0.636)$</td>
</tr>
<tr>
<td>mantle</td>
<td>total</td>
<td>$-2.407 \pm 0.001 \ (0.433)$</td>
</tr>
<tr>
<td></td>
<td>transverse</td>
<td>$-2.417 \pm 0.001 \ (0.491)$</td>
</tr>
<tr>
<td></td>
<td>compressional</td>
<td>$-2.471 \pm 0.001 \ (0.624)$</td>
</tr>
<tr>
<td>tail</td>
<td>total</td>
<td>$-2.407 \pm 0.001 \ (0.390)$</td>
</tr>
<tr>
<td></td>
<td>transverse</td>
<td>$-2.470 \pm 0.001 \ (0.464)$</td>
</tr>
<tr>
<td></td>
<td>compressional</td>
<td>$-2.406 \pm 0.001 \ (0.625)$</td>
</tr>
</tbody>
</table>
for hydrodynamic ($\alpha = -5/3$) and magnetohydrodynamic (MHD) turbulence ($\alpha = -3/2$) and the mantle and tail region even more smaller indices meaning that the spectral power decreases more rapidly there. The spectral slopes observed by Vörös et al. (2008a,b) for a case study along the Venus Express trajectory and a statistical analysis of 20 days in the magnetosheath (not close to boundaries) are $\alpha \approx -1$ (termed as noisy fluctuations), near the terminator and in the nightside near-planet wake $\alpha \approx -2.5$ (termed as wavy structures), and close to boundaries $\alpha \approx -1.6$ (termed as turbulent regions). Hence, our observations of a much longer time interval are rather similar in the tail and mantle region, but differ in the magnetosheath. Different behaviour of the transverse and compressional indices indicate that an anisotropy develops with increasing frequencies which tends to be most pronounced in the dayside magnetosheath. Espley et al. (2004) presented a statistical study of low-frequency magnetic field oscillations in the Martian magnetosheath, the magnetic pileup region, and the tail using observations of the magnetometer/electron reflectometer (MAG/ER) experiment on board Mars Global Surveyor (MGS). Below the local proton gyrofrequency they found waves in the dayside magnetosheath which are predominantly compressional and elliptically polarised with wave vectors that have large angles relative to the mean magnetic field. These oscillations were identified as mirror mode fluctuations. In the nightside magnetosheath they observed waves which are predominantly transverse and elliptical, propagating at smaller angles relative to the mean field. The waves were associated with ion/ion-resonant instabilities arising from counter-streaming plasma populations like solar wind pickup ions of planetary origin. Waves in the Martian magnetic pileup region and tail have considerably smaller amplitudes with linear polarisation and oblique propagation directions. They may be a mixture of different wave modes. The intensity of the oscillations was not presented in their study.

Our dayside observations at Venus reveal similar results in comparison to the wave properties in the Martian magnetosheath, except for the fact that the compressional fluctuations are not dominating at Venus. Espley et al. (2004) interpret their observed fluctuations as mirror mode waves, but they also admit that this interpretation is in conflict with the observation of a moderate elliptical polarisation of the waves, as theoretical studies suggest that mirror modes are linearly polarised. But they argue that elliptically polarised mirror mode waves have also been observed in Earth’s magnetosheath. Volwerk et al. (2008a,b) detected mirror mode-like structures in Venus’ dayside magnetosheath so that the properties of mirror modes may give a contribution to our statistical results. On the other hand, Luhmann et al. (1983) suggested that magnetic field fluctuations may be generated in the vicinity of the quasi-parallel portion of the bow shock by plasma instabilities and are convected downstream through the magnetosheath. Indeed, this is an agreement with the results of numerical simulations by Winske (1986) who studied the origin of large magnetic fluctuations in the magnetosheath of Venus and concluded that the most likely source of these waves is the bow shock itself. But the numerical simulations have also shown that waves could be generated by direct interaction of the solar wind with oxygen ions of planetary origin which tends to generate right-handed polarised waves, whereas the bow shock related waves would generate left-handed polarised waves. However, the simulation by Winske (1986) is performed in an idealised situation and our results of the sense of polarisation can be subject to an uncertainty due to the Doppler shift. As already mentioned in Sect. 3.3 upward propagating waves could reverse their senses of polarisation. Assuming that the waves are mainly bow shock generated and propagate downstream one may conclude that right-handed and left-handed wave generation mechanisms are balanced as our observations show that the senses of polarisation are rather mixed. At Venus the average Parker spiral angle is about 35° (Luhmann et al., 1997). Thus, the most developed quasi-parallel bow shock geometry in the ecliptic plane (dusk sector) with angles between the bow shock normal $n$ and the interplanetary magnetic field (IMF) $B$ of less than 10°, we estimate to appear at moderate solar zenith angles (SZAs; the SZA is the angle between the x-axis and the line connecting the point of origin with a point on the bow shock in the VSO coordinate system) of about 30° to 70°. In our cylindrical coordinate system the wave intensity related to quasi-parallel bow shock processes would occur in the same angle range, but due to the averaging the wave intensity may be reduced. We notice a localisation of the majority of red-coloured bins in Fig. 8 between 30° and 70° SZA. Altogether, the enhanced wave intensity downstream of the bow shock is remarkable. Therefore, we refer a substantial part of the wave activity to bow shock related processes and interpret that, in particular, the wave generation could be associated with the quasi-parallel shock itself as also Luhmann et al. (1983) suggested. However, the bins showing the largest wave intensity at low SZAs are closer to the UMB than to the bow shock suggesting that wave sources may also exist in the magnetosheath and in the vicinity of the UMB, respectively. The generation of mirror mode waves in Earth’s magnetosheath is believed to occur not only at the bow shock, but also within the magnetosheath (Tátrallyay and Erdős, 2002). The origin and evolution of mirror mode structures observed at Venus (Volwerk et al., 2008a,b) may be similar and mirror modes are thus a candidate for waves generated downstream of the bow shock. A differentiation between the quasi-parallel and quasi-perpendicular bow shock regions based on Venus Express measurements of the IMF direction is beyond the scope of this paper and will be subject of future work. A first case study has recently been presented by Du et al. (2009).

The wave properties of the nightside magnetosheaths at Venus and Mars also show similarities: at both planets the power or amplitude is more in the transverse direction than...
in the compressional one, the oscillations tend to be elliptical, and the propagation directions are below 45° relative to the mean field. Espley et al. (2004) refer the observations at Mars to ion/ion-resonant instabilities.

Finally, the tail and mantle regions of Venus show a wider range of observations. This is also similar to the Martian case where a mixture of wave modes are believed to exist. Boundary related processes and current systems (e.g. the ionospheric current system) may become more important there and instabilities may cause a variety of wave modes.

The presented statistical analysis of the low-frequency magnetic field fluctuations reveals first-order results of the wave characteristics in specific regions. They show only the dominating waves properties in different interaction regions and provide a general picture of possible wave modes in Venus’ solar wind interaction region. While much of our discussion assumes MHD wave modes, we note that more complex kinetic plasma models take account of temperature anisotropies and non-Maxwellian velocity distributions which lead to various micro-instabilities and additional waves modes. For anisotropic proton-electron plasmas Gary et al. (1993) argue several low-frequency plasma instabilities. For non-Maxwellian plasma distributions Gary (1991, 1993) also present possible wave generation mechanisms. Case studies give a detailed view of the wave modes and will be an interesting issue of future work using Venus Express data. In this paper we restrict our analysis to the statistical point of view, as it is motivated by a comparative study to Mars. The observations of the wave properties show generally results which emphasise the similarities of the interaction of the planets with the solar wind assuming that the observed wave properties are attributed to the same generation processes.

Concerning the post-terminator waves observed by Brace et al. (1983) at Venus, we do not see a relation to our observations at the moment since these waves are observed below 200 km altitude, while the lowest altitude of the Venus Express spacecraft was about 250 km in the data set we analysed. But Brace et al. (1983) discuss as one possible source of the waves turbulence at higher altitudes and thus it will be interesting to look whether this phenomenon and observations can be connected or not once data of lower altitudes are available.

4.2 Wave intensity and Alfvénic/magnetosonic boundary

One possibility to explain the localisation of enhanced wave activity in the dayside magnetosheath may be spatial variations of the Mach numbers in Venus’ solar wind interaction region. The solar wind upstream of the bow shock is characterised by supersonic, super-Alfvénic, and supermagnetosonic velocities (e.g. Luhmann et al., 1997). The bow shock is a fast magnetosonic shock wave (e.g. Phillips and McComas, 1991) and thus the solar wind flow is slowed down to submagnetosonic velocities, when crossing the shock wave. Further downstream of the shock the flow should reach again supermagnetosonic velocities at a “magnetosonic” line similar to the so-called sonic line inferred from numerical simulations by Spreiter and Stahara (1980). A similar behaviour may occur for the Alfvén Mach number in MHD. Downstream of the bow shock also the Alfvén Mach number may become less than 1, because of the varying magnetic field strength, density, and temperature. In a sub-Alfvénic/submagnetosonic regime waves are not only convected by the flow, but can also propagate upstream and populate the entire region between the bow shock and an Alfvén or a magnetosonic line. In a super-Alfvénic/supermagnetosonic regime the wave energy transport is only in the direction of the background flow. Thus, the transition region from sub-Alfvénic/submagnetosonic to super-Alfvénic/supermagnetosonic flows could represent a reasonable boundary in the wave activity level. Without further knowledge of parameters like the plasma temperature and the density the location of such a boundary and the spatial distributions of the Mach numbers remain speculative for the moment. It can be investigated in more detail with a comprehensive plasma moment data set which is yet not provided by the Analyser of Space Plasmas and Energetic Atoms (ASPERA-4) on board the Venus Express spacecraft. However, an estimate of the Alfvén Mach number we determined on the basis of preliminary ASPERA-4 density and the magnetic field observations. It indicates an Alfvén Mach number greater than 1 in Venus’ magnetosheath and thus waves with velocities up to the Alfvén velocity should be convected with the plasma flow.

4.3 Wave intensity along streamlines

As a further possibility to interpret the observed wave intensity distribution, we discuss the geometric effect on the decay of the waves with the hypothesis that a spatial variation of the wave intensity is due to varying distances between streamlines and the change of the flow velocity. Testing this hypothesis requires knowledge of the magnetosheath flow pattern. For this, we apply an analytical streamline model to describe the flow in the magnetosheath which allows us to trace the evolution of the intensity along different streamlines in the statistical sense. We use the model of a hydrodynamic, irrotational flow (e.g. Vallentine, 1967) past a cylinder for the dayside magnetosheath continued by a flow parallel to a straight line for the nightside. This model was already used successfully by Luhmann et al. (1983) tracing magnetic field fluctuations along streamlines back to the quasi-parallel portion of the bow shock. They also pointed out that the model streamlines are in good agreement with that of the gasdynamic model of Spreiter and Stahara (1980) for the solar wind interaction with Venus. We note here that the nightside mantle boundaries of Martinez et al. (2009) are modelled in a different way than the dayside boundaries and a continuous
transition is lacking at the terminator which cannot be reproduced by the analytical streamline model. As our focus lies on the dayside magnetosheath and the intensity on the nightside is generally much lower, no major deviations are expected by considering a straight streamline parallel to the $x'$-axis. The streamline functions $\Psi$ are given as

\begin{align}
\Psi_d &= v y' \left(1 - \frac{r^2}{x'^2 + y'^2}\right), \\
\Psi_n &= v y',
\end{align}

for the dayside (d) and the nightside (n), respectively. $v$ is the nominal velocity (100 km/s), $r$ is the radius of the obstacle, and $x'$, $y'$, $z'$ are the Cartesian coordinates. The velocity vector is tangential to the streamline at all points (which is the definition of a streamline). Furthermore, we define the velocity potential functions $\Phi$ given as

\begin{align}
\Phi_d &= v y' \left(1 + \frac{r^2}{x'^2 + y'^2}\right), \\
\Phi_n &= v x',
\end{align}

for the dayside and the nightside, respectively. The velocity potential lines are defined such that, when differentiated with respect to distance in any particular direction, it yields the velocity in that direction. The velocity potential lines are perpendicular to the streamlines.

Figure 9 shows the spatial distribution of the wave intensity connected to the streamlines. The intensity is averaged over two neighbouring streamlines and velocity potential lines.

Considering now a geometric effect on the wave intensity decay along a streamline $I(s)$ due to the varying velocity and cross sectional area, the continuity equation of a stationary flow as a function of the distance along the streamline $s$ is given as

$$I(s) v(s) A(s) = \text{const.},$$

where $v(s)$ is the velocity and $A(s)$ the cross sectional area of the flow line. Here, we assume that there is no wave source or sink in the magnetosheath. It is also assumed that the waves are generated in the bow shock region only and wave damping is restricted to frequencies close to the proton cyclotron frequency that is why the damping is not considered here. Equation (9) determines theoretically the evolution of the wave intensity and this can be compared to the observations. Here, the flow velocity $v(s)$ and the cross sectional area $A(s)$ can be estimated using the proposed flow model. Figure 10 shows examples of the evolution of the intensity along four different streamlines. The intensity evolution estimated from the continuity equation remains almost constant along the streamlines (solid lines), while the observed intensities (asterisk symbols) show a steeper decay. However, the observed wave intensity does not decrease monotonically.
with increasing distance from the bow shock. At first, the intensity increases slightly and only then the decrease begins (streamlines 2 to 4; at streamline 1 no observations are available close to the bow shock) which may indicate also that a wave source further downstream of the bow shock exists. Generally, Fig. 10 suggests that the variations of the velocity and the cross sectional area along the streamlines are too small to account for the observed spatial decay of the wave intensity. Since the estimated intensities are almost constant, the changing velocity and cross sectional area play only a minor role in the evolution, even if one would assume that a wave source is located in the magnetosheath. Then, the initial value of the estimated intensity in Fig. 10 would change, but the almost constant curve shape would not be changed significantly. For this reason, we rule out the effect of velocity and cross section variations to explain the rapid spatial decay of the wave intensity in the magnetosheath.

\[ E \propto t^{-\lambda}, \]  

(10)

where the exponent \( \lambda \) is characteristic for the turbulent system. According to Kolmogorov (1941) one can derive an exponent of \( \lambda = 10/7 \), while for MHD turbulence the exponent is \( \lambda = 2/3 \) (Biskamp, 2003). These exponents are derived under the assumption of self-similarity behaviour in turbulence. More complex models are also possible which consider various ratios of kinetic to magnetic energy and they provide further solutions of Eq. (10). Note that the exact solution of Eq. (10) is \( E = E_0(t - t_0)^{-\lambda} \), where the constant \( t_0 \) is of the order of the initial eddy-turnover time and that is why the power law decay becomes visible only at sufficiently large times \( t \gg t_0 \) (Biskamp, 2003).

Since the flow velocity in the magnetosheath is supposed to be super-Alfvénic and the fluctuations are more Alfvénic (transverse), we relate the distance \( s \) along a streamline to the elapsed time since the bow shock crossing by using Taylor’s hypothesis

\[ t = \frac{s}{v(s)}. \]  

(11)

We note that this a reasonably good approximation for not propagating waves like mirror modes or downstream propagating waves in the plasma frame of reference, but the time scale would increase in case of upward propagating waves and Taylor’s hypothesis should be used with caution. The measured intensity \( I \) is proportional to the magnetic energy density \( E \) of the fluctuations in the frequency range 30 to 300 mHz if normalised by a constant \( C \) such that \( E = CI \) with \( C = N \Delta f (2\mu_0)^{-1} \) (\( N \): Number of frequency samples over which has been averaged, \( \Delta f \): frequency resolution in the spectra, \( \mu_0 \): permeability of free space).

Figure 11 shows the evolution of the intensity with time after the bow shock crossing. A power law fitting to the decaying part of the observed intensity evolution gives a good agreement with the data. Some parts in the measurements show approximately a constant behaviour (data points closest to the bow shock, particularly in the third panel). They
may be related to the constant $t_0$ which is of the order of a few tens of seconds. The observed exponents $\lambda$ vary from $-1.7$ to $-3.9$ and are steeper than the exponents predicted by theoretical models of turbulence, but nevertheless the observations exhibit the power law decay and it is suggestive of turbulent decay. Considering wave sources in the magnetosheath, the $t = 0$ point has not to be located necessarily at the bow shock, but can be located further downstream. This would shift the data in Fig. 11 to the left leading to a lower exponent of the power law. Then, the power law exponents would probably be more consistent with the theoretical exponents and therefore, one may consider further wave sources possible. Of course the theoretical models describe an idealised picture of turbulence (spatially unbounded, etc.) and a realistic model would be needed for a quantitative study (considering e.g. the magnetosheath geometry, the bow shock shape and the solar wind conditions). We note in this context that it is also worthwhile to consider in future studies, performing a more detailed discussion on turbulent processes, the spatial distribution and the evolution of the relative amplitude $\Delta B / B$.

5 Conclusions

We performed a statistical analysis of low-frequency magnetic field fluctuations in the frequency range 30 to 300 mHz in the Venusian solar wind interaction region. The magnetic field data set was obtained by the fluxgate magnetometer on board the Venus Express spacecraft. The observations cover the low-altitude magnetosheath as well as the mid-magnetotail. The observations reveal similar wave properties in the magnetosheaths of Venus and Mars as well as their tail regions, suggesting a similar solar wind interaction between the two planets. However, only a global picture of the dominating wave properties is provided which is suitable to compare the observations at both planets, but we are not resolving individual wave modes. This is left to future studies. We also note that the wave propagation directions and the wave properties in the plasma frame of reference are not determined in our measurements and this makes it difficult to get clearer results. This is due to measurements from a single spacecraft only.

The wave intensity reaches a maximum in the dayside magnetosheath and drops rapidly towards the terminator region. The further regions do not show significant wave intensities. Different hypotheses have been considered in order to explain our observation. The influence of varying Mach numbers can not be evaluated accurately at the moment. It has to be studied in more detail in the future with a comprehensive plasma moment data set. A geometric effect plays only a minor role. A reasonable explanation is freely evolving or decaying turbulence, because of the power law behaviour. But the quantitative agreement is poor with the freely decaying turbulence model which may probably be improved by taking wave generation in the magnetosheath into account. On the other hand, further mechanisms like damping could be responsible for the loss of energy. Perhaps the decrease in the magnetic field fluctuations may be compensated by a relative increase in the electric field fluctuation as in high-frequency phenomena in the solar wind (Bale et al., 2005). Unfortunately, this can not be verified by Venus Express, since the spacecraft is not equipped with an electric field detector. Also, a dissipation process could take place like Landau or cyclotron damping. This will be studied using plasma moment data once they are available soon.

In summary, we conclude that the observations suggest the convection of waves by the plasma flow. Doubtless, waves are generated at the bow shock or in its vicinity. But the observations indicate also wave sources within the magnetosheath and thus it may occur that beside the bow shock region waves are also generated within the magnetosheath and the vicinity of the UMB, respectively.

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