Estimates of eddy turbulence consistent with seasonal variations of atomic oxygen and its possible role in the seasonal cycle of mesopause temperature

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Received: 5 April 2010 – Revised: 18 October 2010 – Accepted: 19 October 2010 – Published: 18 November 2010

Abstract. According to current understanding, adiabatic cooling and heating induced by the meridional circulation driven by gravity waves is the major process for the cold summer and warm winter polar upper mesosphere. However, our calculations show that the upward/downward motion needed for adiabatic cooling/heating of the summer/winter polar mesopause simultaneously induces a seasonal variation in both the O maximum density and the altitude of the [O] peak that is opposite to the observed variables generalized by the MSISE-90 model. It is usually accepted that eddy turbulence can produce the [O] seasonal variations. Using this approach, we can infer the eddy diffusion coefficient for the different seasons. Taking these results and experimental data on the eddy diffusion coefficient, we consider in detail and estimate the heating and cooling caused by eddy turbulence in the summer and winter polar upper mesosphere. The seasonal variations of these processes are similar to the seasonal variations of the temperature and mesopause. These results lead to the conclusion that heating/cooling by eddy turbulence is an important component in the energy budget and that adiabatic cooling/heating induced by upward/downward motion cannot dominate in the mesopause region. Our study shows that the impact of the dynamic process, induced by gravity waves, on [O] distributions must be included in models of thermal balance in the upper mesosphere and lower thermosphere (MLT) for a consistent description because (a) the [O] distribution is very sensitive to dynamic processes, and (b) atomic oxygen plays a very important role in chemical heating and infrared cooling in the MLT. To our knowledge, this is the first attempt to consider this aspect of the problem.

Keywords. Meteorology and atmospheric dynamics (General circulation; Middle atmosphere dynamics; Turbulence)

1 Introduction and background

The thermal balance of the mesosphere and lower thermosphere (MLT) is controlled by radiative heating due to absorption of solar UV radiation by O$_2$ and O$_3$, by chemical heating from exothermic reactions, by radiative cooling associated with infrared emission of CO$_2$, and heating and cooling induced by dynamic processes. The latter includes compression/expansion caused by downward/upward motion associated with the gravity wave-driven meridional circulation, as well as direct heating due to the gravity wave dissipation and turbulent diffusion from breaking gravity waves and/or the Kelvin–Helmholtz instability (KHI), caused by sheared flow.

The various contributions of different dynamic processes to the energy budget of MLT are still in much debate (Dunkerton, 1978; Hines, 1997; Medvedev and Klaassen, 2003; Becker, 2004; Akmaev, 2007; Becker and McLandress, 2009). According to an overview of chemical and physical processes presented by Smith (2004), adiabatic heating/cooling caused by sinking/upwelling is the most important process and provides the unusual temperature structure of a warm winter/cold summer in the upper mesosphere. According to the SOCRATES model used by Smith, the maximum adiabatic heating is found to be 16 K/day in the winter polar mesosphere and the maximum adiabatic cooling rate is found to be $-14$ K/day during the summer polar mesopause. This cooling/heating is caused by mean vertical motions with a magnitude of $\pm 2$ cm/s. In this model, eddy diffusive heating is absent in the summer mesopause. According to the SOCRATES model, the cold summer mesopause is caused entirely by adiabatic cooling, with maximum upward motion (expansion) occurring at the altitude of the mesopause. During the winter mesopause, adiabatic heating only takes place below the mesopause since the maximum of the downward motion (compression) occurs below the mesopause. In this case, chemical heating is
important (Berger and von Zahn, 1999). As seen from Fig. 1, agreement exists between the height profiles of the temperature calculated by the model and given by the MSISE-90 model (Hedin, 1991) at altitudes below the polar winter mesopause, but the model and the MSISE-90 data are very different above the mesopause. The agreement between the SOCRA TES and MSISE-90 models is much worse around the polar summer mesopause. The strong discrepancies between the SOCRA TES models and the empirical model MSISE-90 are as follows:

1. The SOCRA TES model cannot reproduce one of the main features of the mesosphere-lower thermosphere (MLT): the decrease in the lower boundary of the thermosphere from winter to summer. It is very difficult to believe that the lower boundary of the thermosphere is located below 80 km in summer, as seen in Fig. 1.

2. In Fig. 2, a strong discrepancy exists between the calculated temperatures and the temperatures given by the MSISE-90 model at middle latitudes.

3. According to the MSISE-90 model, the latitudinal variation of temperature at the winter mesopause does not exceed 8 K, but this variation is 38 K in the summer mesopause. Also, the MSISE-90 model (see Fig. 3) shows that the maximum decrease in temperature at the summer polar mesosphere from winter solstice to equinox is about 50 K but the maximum increase in temperature in the winter mesosphere is 20 K (also see Fig. 3). A mechanism based on adiabatic heating/cooling cannot explain these asymmetries between the summer and winter mesosphere.

We note also that the SOCRA TES results strongly contradict the heating rate of +10 to +20 K/day determined by (a) in situ measurements of neutral density fluctuations in the summer polar mesopause (Lübken, 1997), and (b) the dynamic cooling rate of −31 K/day associated with the vertical heat transport by dissipating gravity waves in the mesopause region as measured by a Na lidar at the Starfire Optical Range in winter at middle latitudes (Gardner and Yang, 1998).

Fritts and Luo (1995) presented a model for dynamic forcing of the summer polar mesopause circulation and thermal
structure at high latitudes. Dynamic forcing is provided by gravity wave energy and momentum fluxes and their divergences. The model gives a turbulent heating rate of +20 to +25 K/day in the summer polar mesopause that increases with increasing altitude, reaching 60 K/day at 100 km. This high heating requires an upward velocity of 5 cm/s to provide net adiabatic cooling in the summer mesopause.

The Fritts and Luo (1995) model shows that eddy turbulence and vertical motion induced by gravity waves play a very important role in the thermal balance in the upper mesosphere. Gardner and Yang (1998) also showed the importance of gravity wave dissipation in thermal balance in the upper mesosphere.

However, Smith (2004), Hocking (1999), and other authors (for example, Brasseur and Solomon, 1986; Brasseur et al., 2000) argue that the impact of gravity waves is restricted to their induced change in the zonal and meridional wind and, correspondingly, to adiabatic heating/cooling induced by the downward/upward motion and that this is the main source of the temperature seasonal variations in the upper mesosphere. Hocking (1999) and Smith (2004) do emphasize many uncertainties in the relationship of turbulent energy dissipation, turbulent heat transport, and diffusion. Hocking notes two main problems: “first, turbulence is very intermittent both temporally and spatially, and very often occurs in thin layers in the middle atmosphere. These thin layers are often separated by regions that are either only weakly turbulent or even laminar. Secondly, the processes which induce diffusion can themselves be scale dependent.” These problems are very important when describing short-time variations in the temperature. However, when we try to model such long-time seasonal variations, we need mean values for the statistically steady turbulent motion. Numerous experimental data on eddy turbulence exist (see, for example, Fukao et al., 1994; Lübken, 1997; Hill et al., 1999), and these data facilitate inferring the mean values of eddy turbulence and their long-time seasonal variations. It is important to emphasize that the meridional wind and wind shears are very intermittent in altitude, as can be seen from the measurements (Larsen, 2002), meaning that vertical motion driven by the meridional wind is very intermittent as well. Finally, no available measurements of the vertical velocity exist, and estimates of this velocity from divergence of the horizontal wind are very difficult. However, there are many measurements of the eddy diffusion coefficient.

Several approaches to estimating the heating rates corresponding to turbulent dissipation of gravity wave kinetic energy were developed recently (Medvedev and Klaassen, 2003; Becker, 2004; Akmaev, 2007; Becker and McLandress, 2009). The heating rates estimated by Becker (2004) for summer conditions are similar to the heating rates measured by Lübken (1997), but Becker’s peak value is less by a factor of about 2 and the peak height is smaller by 7 km than Lübken’s measured parameters. However, the estimated heating rates for winter conditions are very different from the measured values. There are similar differences between the eddy diffusion coefficients calculated by Becker (2004) and measured by Lübken (1997). Akmaev (2001) simulated an eddy diffusion coefficient peak altitude of 110 km for January that is higher by 17 km than the peak altitude measured by Lübken (1997).

To our knowledge, the models explaining the cold summer and warm winter mesopause do not consider the effect of dynamic processes on the distribution of atomic oxygen, which plays an important role in chemical heating and infrared cooling in the upper mesosphere. For example, the extended version of the Canadian Middle Atmosphere Model presented by Fomichev et al. (2002) includes eddy and molecular diffusion and vertical advection, which strongly influence the [O] distribution. However, the model uses vertical profiles for [O] given by the MSISE-90 model. The infrared radiation of the 15-μm CO₂ band is the main cooling process in the upper mesosphere. The quenching of excited CO₂ by atomic oxygen is one of the most important factors determining this cooling. The authors tried to reduce the cooling rate error below 5% in the upper mesosphere. However, the variations in atomic oxygen, induced by the dynamic processes included in the model, can change this cooling rate by a few times. Note that atomic oxygen is the main constituent in the thermosphere and that the O thermospheric density strongly depends on the altitude of the peak density in the upper mesosphere. The altitude of the peak density is controlled by the dynamic processes responsible for the temperature anomaly in the mesopause.

The goal of this paper is to consider the contradiction between the observed seasonal variations of atomic oxygen density distributions in the upper mesosphere and lower thermosphere (MLT) and the impact of upward/downward motion, responsible for the cold summer and warm winter mesopause, on the [O] distribution. We estimate the impact of eddy turbulence and vertical motion on the [O] distribution, derive the eddy diffusion coefficient corresponding to the seasonal variations of [O] corresponding to the experimental data associated with the MSISE-90 model (Hedin, 1991), and then, using these results, estimate the contribution of heating/cooling of eddy turbulence in the thermal balance of the upper mesosphere and the seasonal variations of mesopause temperature. To our knowledge, this is the first attempt to include a minor constituent in testing theories for the cold summer and warm winter mesopause.

2 Impact of eddy diffusion and vertical motion on the [O] distribution

Using the continuity equation, the seasonal variations of the O peak density and the altitude of the [O] peak from summer to winter by a factor of nearly 2.25 and by 4 km, respectively.

This simple approximation describes the main features that impact the [O] height distribution: production, loss, and dynamic processes (eddy turbulence and upward motion). As seen from Fig. 4, an increase in the upward velocity induces an increase in the O density and in the altitude of the [O] peak. A \( K_{\text{ed}} \) increase induces an [O] decrease. The effect of these dynamic processes on the [O] distribution is much stronger than a recombination. But, in general, the results of the numerical solution of Eq. (2) with squared-law recombination and an altitude-dependent coefficient show the same impact of eddy diffusion and vertical motion in the [O] distribution (Vlasov and Davydov, 1982, 1993). In any case, the upward/downward motion in the polar summer/winter mesosphere induces a seasonal variation in the O density and in the altitude of the [O] peak, contrary to the experimental data. Finally, we note that there is no experimental evidence for upward/downward motion in the mesosphere, but there is a set of experimental data on eddy turbulence. Using the numerical model developed by Vlasov and Davydov (1983, 1993) with eddy diffusion coefficients approximated by the formulas close to the coefficients obtained by Lübben (1997), it is possible to reproduce the [O] seasonal variations given by the MSISE-90 model, as seen from Fig. 5. In the next section, we estimate the heating/cooling corresponding to the eddy diffusion coefficient used in calculations of the [O] seasonal variations. Note that the eddy diffusion coefficients should be increased by a factor of 2–3 to obtain [O] profiles similar to the profiles shown in Fig. 5 if the upward/downward motion corresponding to the adiabatic cooling/heating is included.
3 Heating and cooling by eddy turbulence

There are different approaches and numerical models for estimating the heating/cooling rates induced by the gravity waves in MLT (Medvedev and Klaassen, 2003; Becker, 2004; Akmaev, 2007, 2009; Becker and McLandress, 2009). All models start from gravity waves and then calculate the heating/cooling corresponding to the different dynamic processes induced and driven by gravity waves. Some models estimate the eddy diffusion coefficient, as mentioned in the introduction. However, we start from the eddy diffusion coefficients and try to estimate the heating/cooling rates corresponding to them.

In this case, the heating/cooling rate of eddy turbulence is given by the formula (see Fritts and Luo, 1995)

$$Q_{ed} = \frac{\partial}{\partial z} \left[ K_{ec} C_p \rho \left( \frac{\partial T}{\partial z} + \frac{g}{C_p} \right) \right] + K_{ec} \frac{g}{C_p} \left( \frac{\partial T}{\partial z} + \frac{g}{C_p} \right).$$

where $K_{ec}$ is the eddy heat conductivity, $\rho$ is the undisturbed gas density, $g$ is the gravitational acceleration, $T$ is the temperature, $C_p$ is the specific heat at constant pressure, and $c$ is a dimensionless constant commonly taken to be 0.8 (Lübken, 1997; Hocking, 1999). The first term on the right side of Eq. (3) is the heat flux divergence, and the second term is the turbulent energy dissipation rate initiated by the dynamic instability of gravity waves and the action of viscous and buoyancy forces. For example, the first term presents divergence of heat flux corresponding to the heat flux given by Becker (2004) for $P_{ref} = 1$ and the heat flux given by formula (23) in Akmaev (2007). The second term is similar to the total wave energy disposition rate per unit mass, $\varepsilon = K \omega_B^2 (1 + P)$, given by Akmaev (2007) where $P$ may be considered a generalized Prandtl number and $\omega_B^2$ is the buoyancy frequency (Akmaev, 2007). There is great debate about the value of the turbulent Prandtl number. First of all, this problem is due to different assumptions about gravity wave energy transport and dissipation and localized or uniform induced turbulence. However, this problem is not within the scope of this paper. We restrict our calculations to only different values of $c$.

Around the mesopause, the temperature gradient is small and $\partial K_{ec}/\partial z$ is small for the $K_{ec}$ peak in the mesopause. In this case, Eq. (3) can be simplified to the formula

$$Q_{ed} = K_{ec} g \frac{\partial \rho}{\partial z} + K_{ec} \rho \frac{g^2}{C_p T c}.$$  

By dividing Eq. (4) by $\rho C_v$ (where $C_v$ is the specific heat at constant volume), multiplying by a time equal to one day, $\tau_d$, and using the formulas $\rho = \rho_0 \exp(-z/H)$ and $C_p = (1 + N/2) \kappa / m$ where $H$ is the atmosphere scale, $N$ is a number of freedom degrees, $\kappa$ is the Boltzmann constant, and $m$ is the mean molecular mass, it is possible to transform Eq. (4) into

$$Q_{ed} = \frac{K_{ec} \tau_d}{C_v H} \left[ \frac{1}{(1 + N/2) c} - 1 \right].$$

As seen from Fig. 6, eddy turbulence can heat the mesopause for $c < 0.286$ and cool it for $c > 0.286$. The range of $c$ values can be estimated. The ratio of the turbulent energy dissipation rate due to the action of viscous and buoyancy forces to the transfer rate of kinetic energy from the mean motion to the fluctuating motion, $Q_{ed} = K_{ed} / (\partial u/\partial z)^2$, is determined by the ratio of the Richardson number, $Ri = \omega_B^2 / (\partial u/\partial z)^2$, to the turbulent Prandtl number, $P = K_{ed} / K_{ec}$. In the case of mean motion, $c$ can be estimated as being equal to $Ri / P$. For the mean wind shears of 20 m/s/km and $\omega_B^2 = (3/5) \times 10^{-4} s^{-2}$, the $Ri$ values are within the range of 0.75–1.25 and the $c$ value is about 1 for $P \approx 1$. The $c$ value decreases with increasing $P$ and turbulent heating can dominate cooling. In any case, we can estimate the sensitivity of turbulent heating/cooling to the influence of wind shear and gravity waves.

Now we consider the heating/cooling caused by eddy turbulence in more detail. The height profile of the temperature given by the MSISE-90 model below the polar mesopause can be approximated by a linear dependence with the gradient $\partial T / \partial z = G = -5.4 K / km$ in summer and $G = -3.2 K / km$ in winter at altitudes 70°S and 70°N, respectively. In this case, the density height distribution is given by the formula

$$\rho = \rho_0 \left( \frac{T_0}{T_0 - G z} \right)^{1 - m g / \kappa G},$$

and the heating/cooling rate given by Eq. (1) can be written as

$$Q_{ed} = K_{ec} \frac{C_p}{C_v} \tau_d \left( \frac{g}{C_p} - G \right) T_0 - G z + \frac{\partial K_{ec}}{\partial z} \frac{C_p}{C_v} \tau_d \left( \frac{g}{C_p} - G \right),$$

Fig. 6. Dependence of heating/cooling by eddy turbulence on the value of $c$, using Eq. (4) for $K_{ec} = 3 \times 10^6 cm^2/s$ and $H = 6 km$.  

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The first term on the right side of Eq. (7) is negative because \( mg/\kappa \) is much larger than \( G \). The second term is positive below the \( K_{ec} \) peak and is negative above the \( K_{ec} \) peak. The eddy diffusion coefficient inferred by Lübken (1997) from measurements of the turbulent energy dissipation rate in the summer polar mesosphere can be approximated by the formulas suggested by Shimazaki (1971):

\[
K_{ec} = K_{ec}^0 \exp\left[ S_1(z-z_m) \right] + \left( K_{ec}^m - K_{ec}^0 \right) \exp\left[ -S_2(z-z_m)^2 \right] \quad z \leq z_m \tag{8}
\]

\[
K_{ec} = K_{ec}^m \exp\left[ -S_3(z-z_m)^2 \right] \quad z > z_m \tag{9}
\]

where \( K_{ec}^m = 1.8 \times 10^6 \text{ cm}^2/\text{s} \) is the maximum of these coefficients, \( z_m = 90 \text{ km}, S_1 = 0.05 \text{ km}^{-1}, S_2 = 0.04 \text{ km}^{-2} \), and \( S_3 = 0.05 \text{ km}^{-2} \). The same approximation is used in the [O] calculations. The height profiles of the heating/cooling rate calculated by Eq. (7) for \( c = 0.3 \) and \( 0.8 \) are shown in Figs. 7, 8, and 9. Note that the summer polar mesopause is located at an altitude of 90 km, according to the MSISE-90 model. Thus, the cooling rates calculated with the eddy diffusion coefficient inferred from measurements are found to be \(-13.5 \text{ K/day} \) and \(-41.5 \text{ K/day} \) for \( c = 0.3 \) and \( c = 0.8 \), respectively, at the mesopause. The strong change in the cooling rate with \( c \) is explained by the strong increase in the dissipative term in Eq. (7) with the \( c \) value decrease.

Using the same approach, we have calculated the heating/cooling rates in the polar winter mesosphere. The height profiles of these rates for \( c = 0.3 \) and \( c = 0.8 \) are shown in Figs. 10 and 11. Note that we increased the altitude of the \( K_{ec} \) peak from 90 km (given by Lübken) to 92 km because, according to the MSISE-90 model, the altitude of the turbopause inferred from the vertical profiles of the \( Ar/N_2 \) ratio is higher in winter than in summer. Comparing the cooling rates in the summer and winter mesopause, it is clear that the turbulent cooling rate in the winter mesosphere is much less than the cooling rate in the summer mesopause. This strong winter-summer asymmetry is well known (e.g., Becker, 2004).

As seen from the results discussed above, eddy turbulence cools the mesosphere at altitudes above and below the \( K_{ec} \) peak for \( c > 0.3 \), and the maximum of this cooling rate is \(-30 \text{ K/day} \) \(-50 \text{ K/day} \) in summer and \(-10 \text{ K/day} \) in winter. Note that the maximum adiabatic cooling rate calculated by the SOCRATES model in the polar summer mesopause is \(-16 \text{ K/day} \), meaning that eddy turbulence can provide the same or an even larger cooling rate than the hypothesized
4 Conclusion

Our results show that seasonal variations of the O density and the altitude of the [O] peak, calculated with upward/downward motion corresponding to adiabatic cooling/heating, are opposite to the observed seasonal variations given by the MSISE-90 model. Eddy turbulence with coefficients close to the values inferred from experimental data by Lübken (1997) can provide the observed seasonal variations of the O density and the altitude of the [O] peak. The heating/cooling by this eddy turbulence is comparable to or larger than adiabatic heating/cooling in the upper mesosphere. The strong impact of upward/downward motion and eddy turbulence on the [O] height distributions requires self-consistent modeling of the O density and temperature because of the important role of atomic oxygen in infrared cooling and chemical heating in the upper mesosphere. The eddy diffusion coefficients should be increased by a factor of 2–3 in order to obtain summer and winter [O] profiles close to the MSISE-90 data if upward/downward motion, corresponding to adiabatic cooling/heating, is taken into account.

Acknowledgements. Topical Editor C. Jacobi thanks E. Becker and another anonymous referee for their help in evaluating this paper.

References


